Modeling excess heat in the Fleischmann-Pons experiment

Peter L. Hagelstein¹ and Irfan Chaudhary²

¹Research Laboratory of Electronics Massachusetts Institute of Technology

²Department of Computer Science and Engineering University of Engineering and Technology, Lahore

Theoretical problem

Although many more results available from experiment, we have enough so far to pose the key theory problem:

How to split up a large ΔE quantum into lots of small quanta?

The major implication of the Fleischmann-Pons experiment is that this is possible and occurs in energy production



Many-spin spin-boson model



C. Cohen-Tannoudji



Two-level systems energy

between two-level systems and oscillator

Earlier versions of the model due to Bloch and Siegert (1940)

Coherent energy exchange



Numerical results for exchanging energy between 1700 oscillator quanta and 100 two-level systems

Thinking about toy model

Coherent multi-quantum energy exchange predicted by toy model

- •Effect is weak
- •Stringent resonance requirements
- •Can exchange up to about 100 quanta coherently
- •Exactly kind of model needed, except energy exchange effect is too weak

Improved toy model



Lossy version of model



Loss term, which allows the system to decay when a large energy quantum is available

Perturbation theory



Many paths from initial to final state, with interference between upper and lower paths

Finite basis approximation for $|n\rangle \otimes |M\rangle \rightarrow |n-5\rangle \otimes |M+1\rangle$

Perturbation theory



Loss channels available for off-resonant states with energy excess, which spoils the destructive interference

Enhancement due to loss



Lossy version of model

- Loss spoils the destructive interference
- Coherent energy exchange rates increased by orders of magnitude
- Much stronger effect
- Model capable of converting 24 MeV to atomic scale quanta

Thinking about PdD



Unfortunately, coupling is too weak because of Coulomb repulsion

Excitation transfer



Indirect evidence from experiment implicates ${}^{A}Z = {}^{4}He$, and theory and experiment suggest that ${}^{A}Z^{*}$ is a localized two-deuteron state

4



$$\hat{H} = \Delta E_{1} \frac{\hat{S}_{z}^{(1)}}{\hbar} + \Delta E_{2} \frac{\hat{S}_{z}^{(2)}}{\hbar} + \hbar \omega_{0} \hat{a} \hat{a}^{\dagger} - i \frac{\hbar}{2} \Gamma(E)$$

+ $V_{1} e^{-G} \frac{2S_{x}^{(1)}}{\hbar} (\hat{a} + \hat{a}^{\dagger}) + V_{2} \frac{2S_{x}^{(2)}}{\hbar} (\hat{a} + \hat{a}^{\dagger})$

This kind of model is first one relevant to experiment

What oscillator modes?



Results from dual laser experiments of Letts, Proc. ICCF14 and ACS Sourcebook vol 2

Dispersion curve for PdD



L E Sansores et al J Phys C **15** 6907 (1982)

Strong-coupling limit

When the coupling between the receiver-side two-level systems and oscillator is strong, then the problem simplifies

$$\Gamma \rightarrow \frac{\hbar \omega_0}{\Delta E(g)} \left| \frac{\langle S, M, n + \Delta n | \hat{H} | S, M + 1, n \rangle}{\hbar} \right|$$

When the excitation transfer step is the bottleneck, then

$$\Gamma = \frac{V_1 \sqrt{n}}{\hbar} \left(\frac{\hbar \omega_0}{\Delta E}\right) e^{-G} \sqrt{\left(S + M\right)\left(S - M\right)}$$

Occupation of virtual levels



Conclusions so far

- •Can model the effect
- •Can see the energy exchange with the lattice
- •Can see excitation transfer
- •Can get rates for both
- •Agreement with experiment if screening energy $\rm U_e$ = 150 eV

Trying out simplified version

$$\frac{d}{dt}N_{D2} + \frac{N_{D2} - N_{D2}^{0}}{\tau_{D2}} = -\Gamma_{0}\sqrt{N_{D2}N_{He}}\Theta(n - n_{thresh})$$
$$\frac{d}{dt}N_{He} + \frac{N_{He} - N_{He}^{0}}{\tau_{He}} = \Gamma_{0}\sqrt{N_{D2}N_{He}}\Theta(n - n_{thresh})$$
$$\frac{d}{dt}n + \frac{n - n_{0}}{\tau_{p}} = \gamma_{J} + \frac{\Delta E}{\hbar\omega_{0}}\Gamma_{0}\sqrt{N_{D2}N_{He}}\Theta(n - n_{thresh})$$

Example: fast He diffusion

Active region: $A = 1 \text{ cm}^2$ $\Delta r = 100 \text{ nm}$

D₂ parameters:

f[vacancy] = 0.25 $f[D_2] = 0.005$ $N[D_2] = 1.8 x 10^{15}$ $\tau_{D2} = 2 x 10^{-8} sec$

⁴He parameters:

 $D_{He} = 1.3 \text{ x } 10^{-14} \text{ cm}^2/\text{sec}$ $\tau_{He} = \Delta r^2/D_{He} = 2.1 \text{ hr}$

Phonon mode: $f_0 = 8.3$ THz O = 20

Deuterium flux: $P_{flux} = 1$ Watt/cm³ $n_{thresh} = 100$

Basic reaction rate: $\Gamma_0 = 1/(3 \text{ hr})$

Evolution of dideuterium, ⁴He







Number of phonons



Addressing the full problem

Start out with full problem

$$E\Psi = H\Psi$$

Then implement picture and approximation through construction of channels

$$\Psi = \sum_{j} \psi_{j} \Phi_{j}$$

Get coupled-channel equations

$$\langle \Phi_i | E \Psi = \langle \Phi_i | H \Psi$$

Coupled-channel equations

Coupled-channel equations that result

$$E\psi_i = H_{ii}\psi_i + \sum_{j\neq i} H_{ij}\psi_j$$

Can put whatever physics that one likes into the channels. Best place to start is with

H = H[nucleons] + H[electrons] + V[strong force] + V[Coulomb]

Coupling

Terms that couple from one channel to another:

$$H_{ij} = \langle \Phi_i | H | \Phi_j \rangle$$

We focus on strong force terms, although others present



Where is the D₂?

Molecular D₂ does not form in bulk PdD

- •Issue is electron density
- •Computation of D₂ in electron gas leads to occupation
- of antibonding states
- •The electron density in PdD is too high
- •If you want D₂, you have to lower the electron density

Bonding and anti-bonding in H₂





W. Kolos and L. Wolniewicz, *J Chem Phys* **43** 2429 (1965)

Pd-H₂ with σ -bonding



In Pd-H₂ d[Pd-H]=1.67 A d[H-H] = 0.81 A

 σ -bonded Pd-H₂ is the ground state of the three-atom system. It is a combination of (4d)¹⁰ ¹S₀ Pd and (1 σ)² ¹S₀ H₂

Electron density of Pd (4d)¹⁰



Electron density at Pd-H distance



Pd-H distance in Pd-H₂ is 1.67 Angstroms, and electron density is 0.033

PdD lattice structure (fcc)



Electron density due to Pd around octahedral site



Cannot form D₂ at O-site

H₂ binds with Pd at 1.67 Angstroms Pd-H separation Electron density at 1.67 Angstroms is 0.33 e/Angstrom³ Electron density at O-site in PdD is 0.081 e/Angstrom³ Anti-bonding orbitals occupied

PdD Host lattice vacancy



Deuterium atoms relax toward host vacancy

Vacancies in host lattice



Vacancies in host metal lattice are thermodynamically favored at high loading





Anodic current

Cathodic current

Conjecture that a small amount of Pd is stripped off during anodic current cycles, and then codeposited during subsequent cathodic loading [most of the Pd in solution is $Pd(OH)_4^{-2}$, Mountain and Wood (1988)]

Electron density with vacancy



Electron density seems low enough

Superposition of atomic electron densities leads to a model electron density of 0.016 e/Angstrom³

- Model electron density is 2x lower than for Pd-H₂
- Would expect D₂ formation near vacancy
- •Would expect relevant literature







1/2(11)

-0.04

K. Balasubramanian et al, J Chem Phys 87 3981 (1987)

Look at Pd density at 1.53 A



Model electron density at 1.53 A is 0.0686 e/Angstrom³

Electron density around vacancy



Nearest O-point no longer a minimum in electron density

Model electron density just right now for H



Compare with Velikova et al (2009) DFT for Pd



Velikova shift corresponds to 0.081 e/Angstrom³ , close to PdH 0.069 e/Angstrom³

Summary (need VASP calculation!)



Expect about 0.4 A shift of D, and about 1 A shift for D₂ location

Summary and conclusions

•Fleischmann-Pons experiment points to new kind of physical process where nuclear energy generated with no energetic reaction products

•Spin-boson model provides analog which can convert a big quantum to a large number of small quanta, but effect is weak

•Lossy spin-boson model can convert a large number a big quantum to a large number of small quanta, and effect is large

More conclusions

•We can construct coupled-channel equations systematically to implement lossy spin-boson type scheme in real physical system

•Detailed modeling now under way