

$^3\text{He}/^4\text{He}$ Production Ratio by Tetrahedral Symmetric Condensation

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AIMS

- Some works report ^3He generation, in addition to ^4He : Arata-Zhang, McKubre et al., and so on
- (1) Based on EQPET model to treat 4-body resonance fusion of mixed H/D state under tetrahedral symmetric condensation (TSC), calculation is made to estimate variation of $^3\text{He}/^4\text{He}$ production ratio as a function of H/D mixing rate.
- (2) Extend the theory to M-nucleus + TSC nuclear interaction
- EQPET: Electronic Quasi-Particle Expansion Theory

Basic Mechanism will be:

- **Formation of Tetrahedral Symmetric Condensate (TSC):**

4 deuterons + 4 electrons make
a transient Bose-type condensation
by 3-dimensionally
constraint squeezing motion

How small can TSC size become?

The Place where TSC is born?

1) **In Natural Gas-Phase** of D_2 (H_2): Very small probability for two $D_2(H_2)$ molecules to make orthogonally coupled state.

→ Possible at very low temperature?

(**Bose-Einstein Condensation**)

2) **In Surface-Lattice** conditions: **O(T)-Sites, Defect/Void, Fractal-surface (adatom + dimer + corner-hole)**

→ (**Dynamic Bose Condensation of TSC**)

Phonon Excitation by Laser

- Dielectric Response Function of Metal:
(Classical Drude-Model for free electron gas)

$$\varepsilon(\omega) = 1 - (\omega_p \tau)^2 / (1 + (\omega \tau)^2)$$
$$\approx 1 - (\omega_p / \omega)^2$$

with $\omega_p = (4 \pi N e^2 / m)^{1/2}$: plasma frequency

which is over UV region ($1E+15$ (1/s))

- 100 % penetration by $\omega > \omega_p$

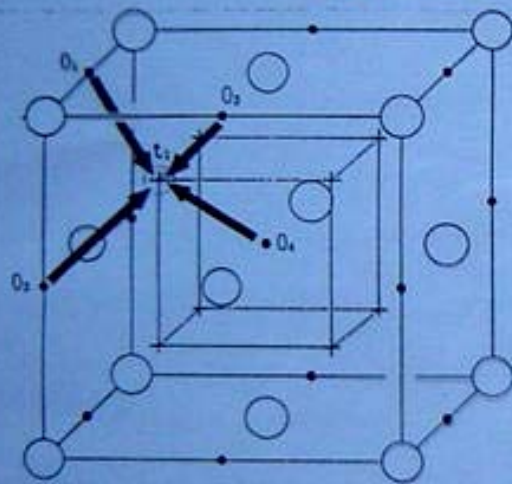
EUV-Laser irradiation can excite phonons inside bulk metal!

D-Cluster Formation in PdD Transient Dynamics by Phonon Excitation

Ref.) A. Takahashi, et al: Fusion Technology, 22 (1995) 71-85

Electron-Plasma-Phonon Coupling and Transient D-Cluster Formation

\Rightarrow [Collision-like Process] \Rightarrow $[R] \approx \frac{dt}{T} \cdot [R]_{\text{steady cluster}}$



- DEUTERON AT OCTAHEDRAL SITE
- + TETRAHEDRAL SITE (Focal Point)
- PALLADIUM

Fig. 1. The FCC lattice of PdD, and squeezing of o-site deuterons onto the t-site.

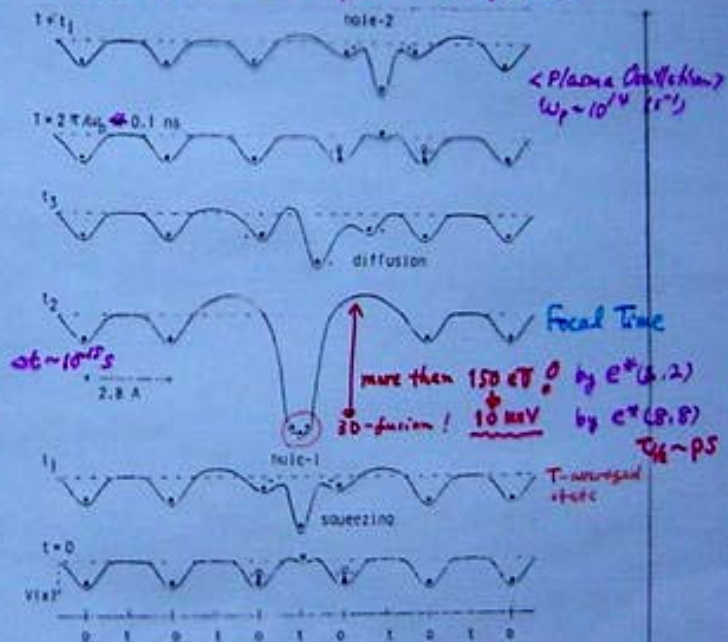
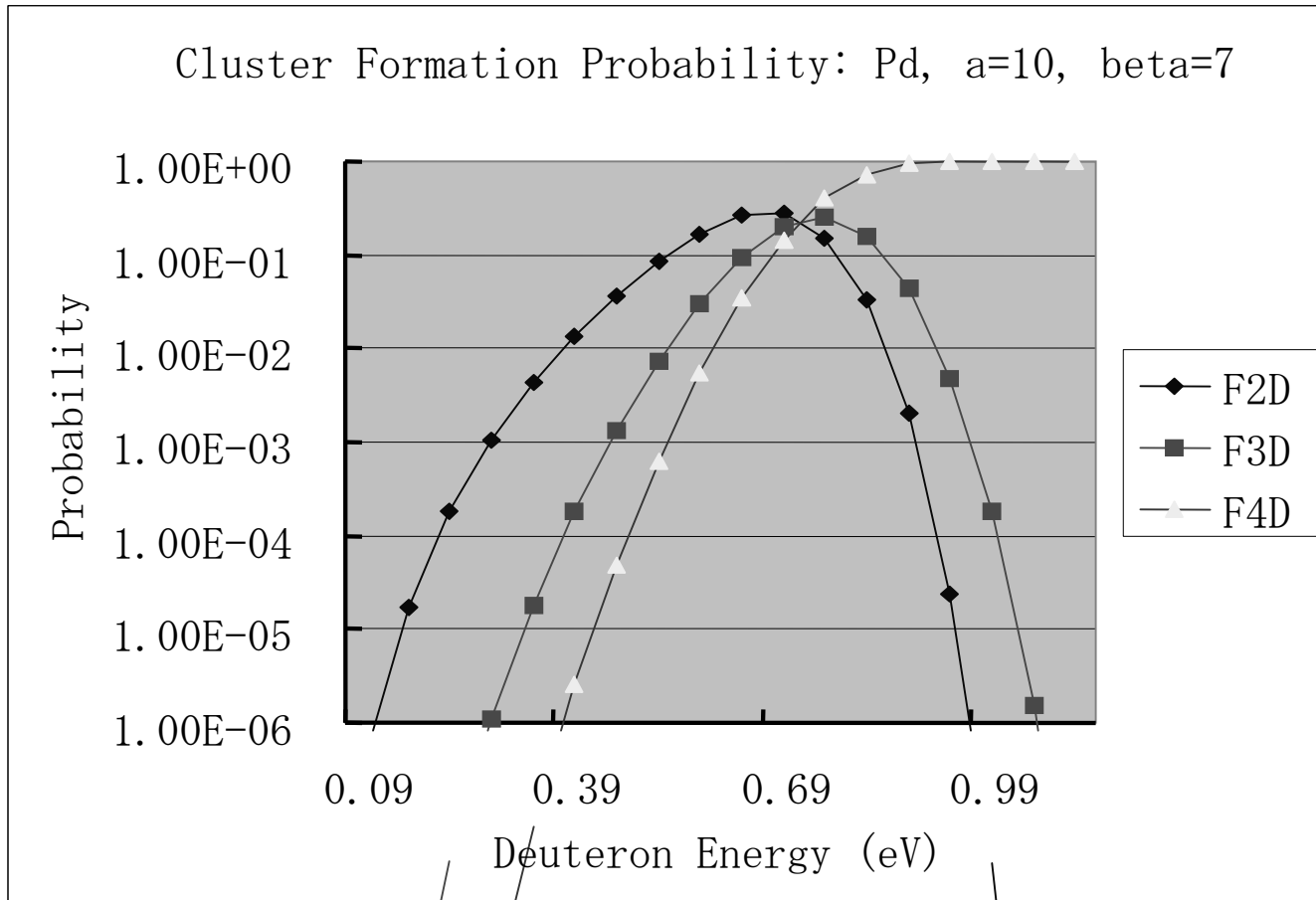


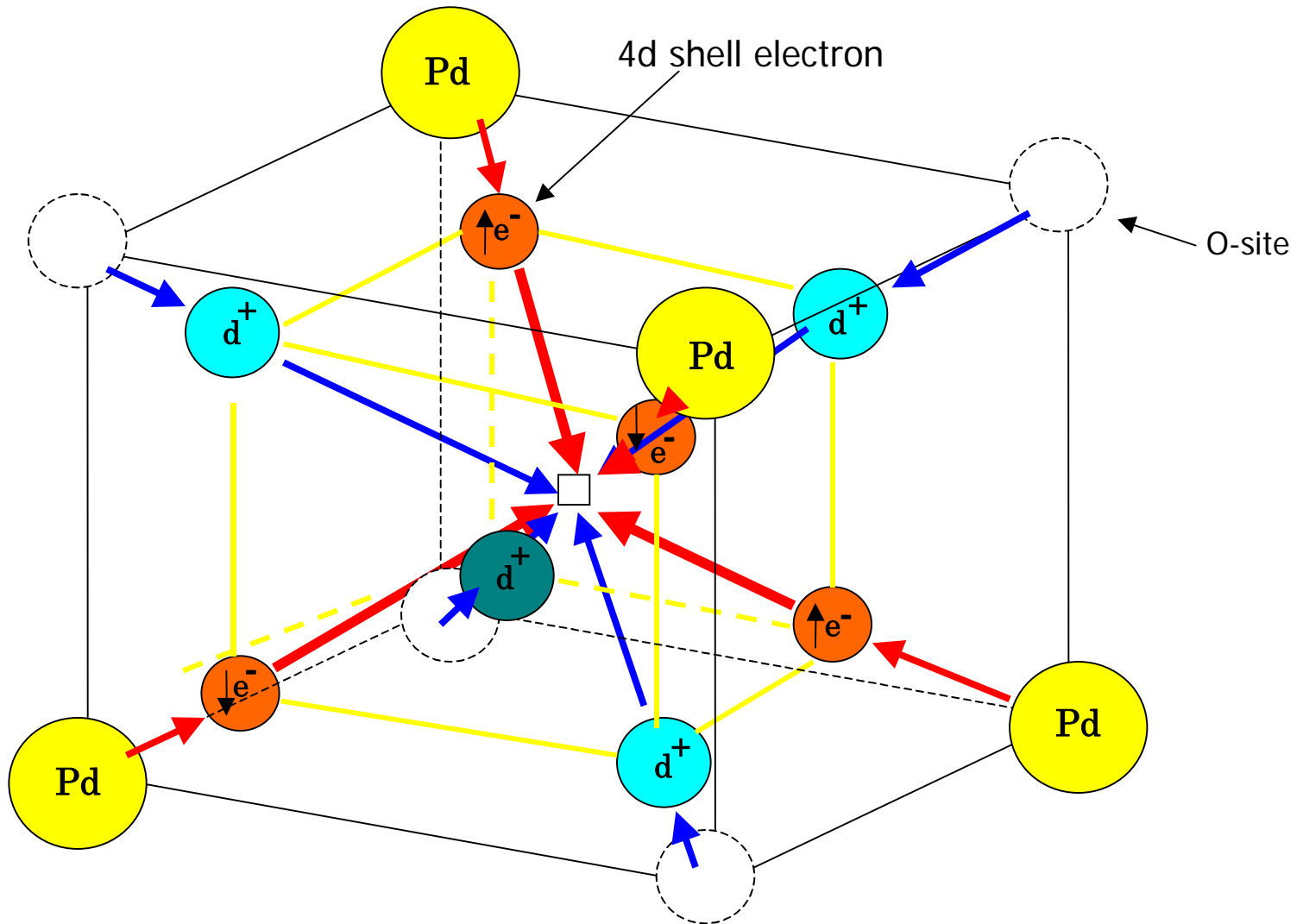
Fig. 3. Image of transient dynamics for microscopic clustering of deuterons.

Cluster Formation Probability in Atomic Level



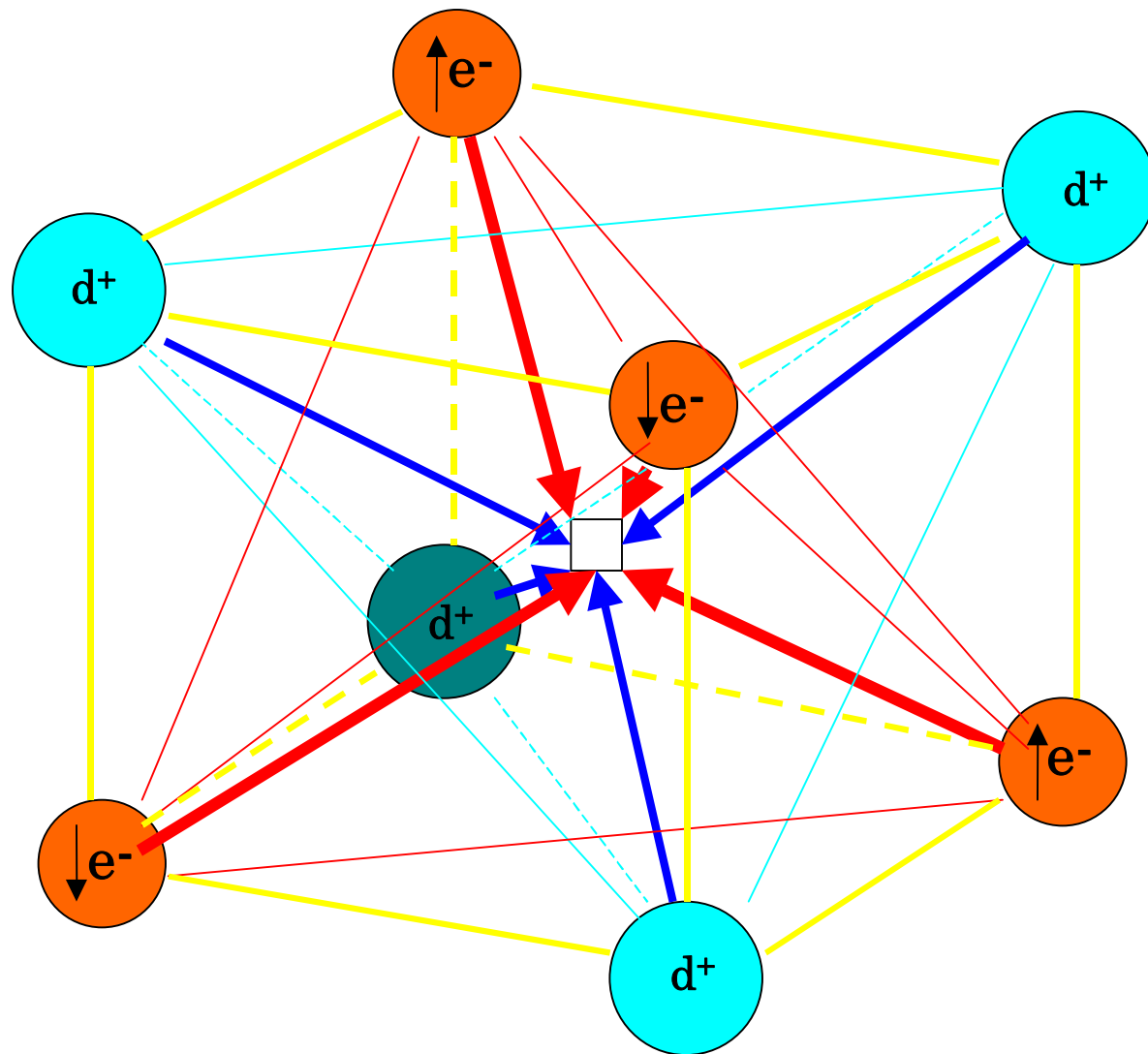
• Calculation by Excitation Screening Model, Fusion Tec. 1991

Tetrahedral Condensation of Deuterons in PdDx



Classical View of Tetrahedral Condensation

Orthogonal Coupling of Two D₂ Molecule makes Miracle !



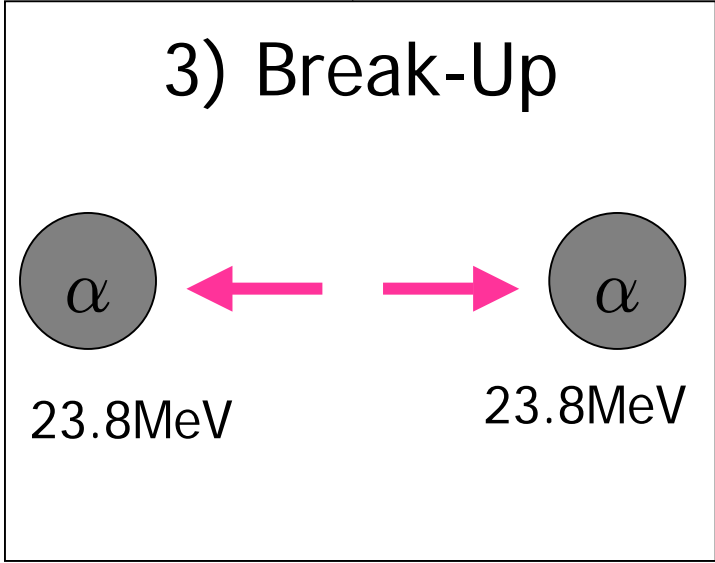
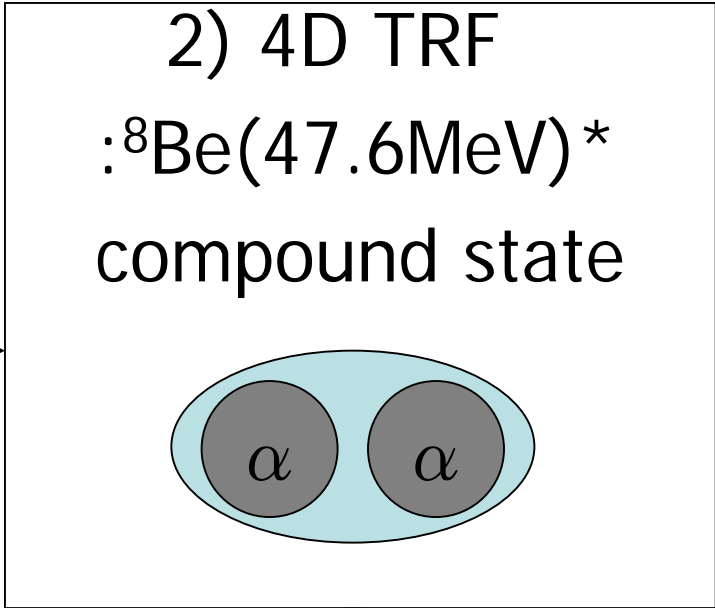
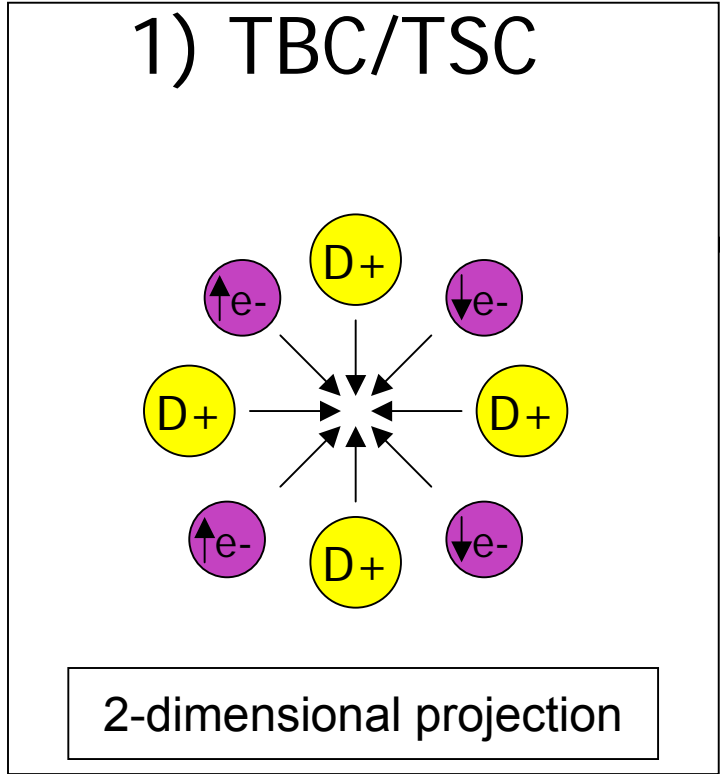
Transient
Combination
of Two D₂
Molecules
(upper and
lower)

Squeezing only
from O-Sites to
T-site

3-dimension
Frozen State for
4d+s and 4e-s

Quadruplet e*
(4,4)

Formation of
Electrons
around
T-site



TBC: Transient Bose Condensation
TSC: Tetrahedral Symmetric Condensation

Assumptions

- By replacing one or two deuterons in 4D TSC with one or two protons
- And assuming same velocities for d and p due to keeping charge-neutrality and energy-minimum in dynamic motion
- We can apply the model to H/D mixed systems

Basic 4-body Fusion by TSC

- $D+D+D+D \rightarrow {}^8\text{Be}^* \rightarrow {}^4\text{He} + {}^4\text{He} + 47.6\text{MeV}$
- $D+D+D+H \rightarrow {}^7\text{Be}^* \rightarrow {}^3\text{He} + {}^4\text{He} + 29.3\text{MeV}$
- $D+H+D+H \rightarrow {}^6\text{Be}^* \rightarrow {}^3\text{He} + {}^3\text{He} + 11\text{MeV}$

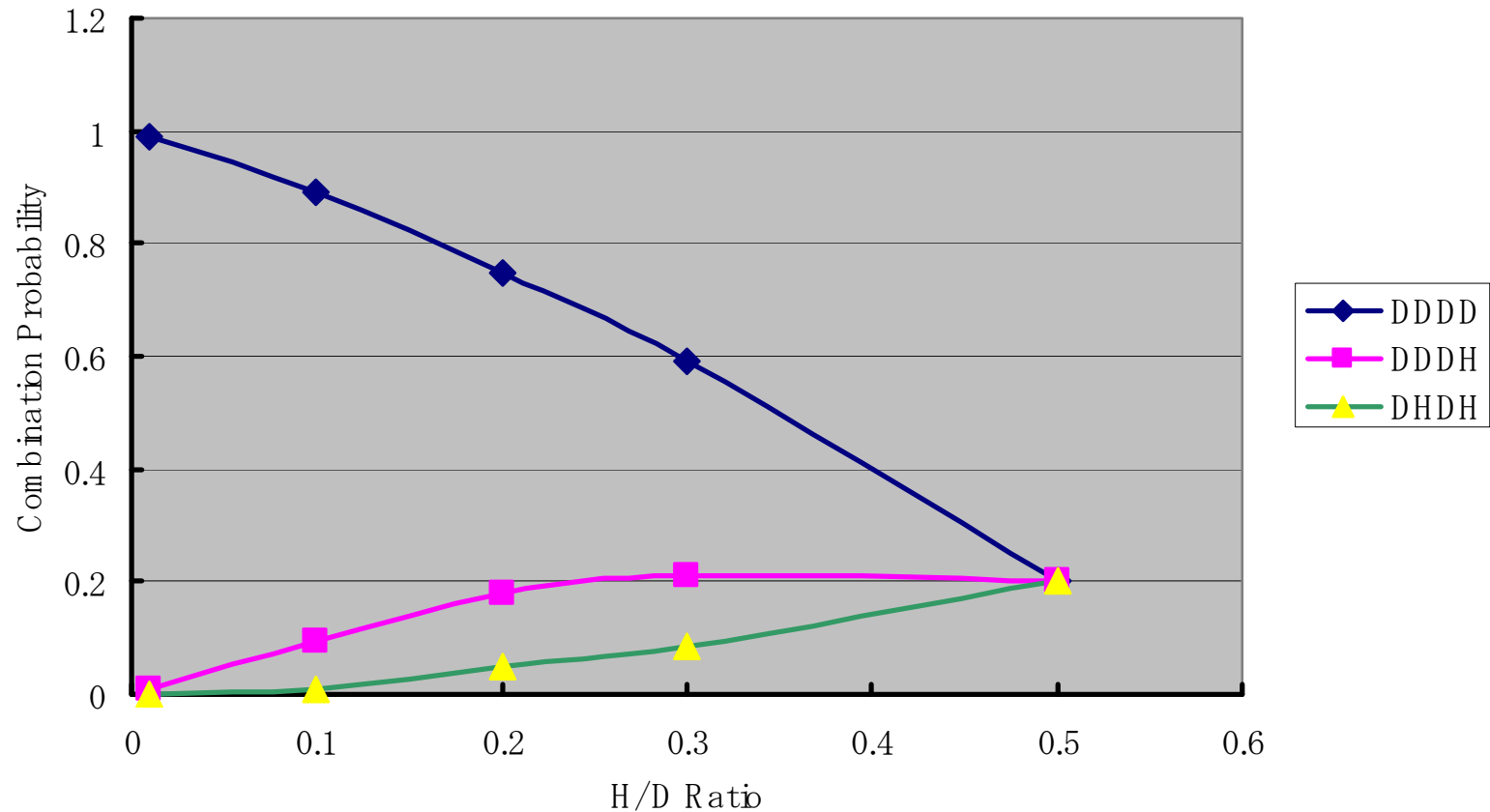
Combination Probability of H/D Mixed TSC Cluster

- $Y = H/D$
- DDDD: $k(1-Y)^4$
- DDDH: $k(1-Y)^3Y$
- DHDH: $k(1-Y)^2Y^2$
- DHHH: $k(1-Y)Y^3$
- HHHH: kY^4

K: Normalize sum probability to be 1.0

Combination Probability for TSC Cluster

Combination Probability for TSC Cluster



Fusion Rate Calculation for EQPET Molecule

- $\lambda_{dddp} = (S_{dddp}/E)vP(dd)P(dp)$
- $\lambda_{dpdp} = (S_{dpdp}/E)vP(dp)P(dp)$
- $S_{dddp} = 10^9 \text{ keVb}$
- $S_{dpdp} = 10^8 \text{ keVb}$
- $P(dp)$: Barrier factor for d-p fusion with dpe^* molecule: $\exp(-2\Gamma_n)$
- $\Gamma_n = \int (V_s - E)^{1/2} dE / ((h/\pi)/(2\mu)^{1/2})$

Fusion Rate for EQPET Molecule

EQP	DDe* (f/s/cl)	DHe* (f/s/cl)	DDDDe* (f/s/cl)	DDDHe* (f/s/cl)	DHDHe* (f/s/cl)
e(1,1)	1E-137	1E-120	1E-252	1E-232	1E-228
e*(2,2)	1E-20	1E-23	1E-17	5E-16	2E-14
e*(4,4)	(1E-16)	(1E-21)	1E-9	1E-10	1E-10

Calculation of Modal Fusion Rate

- Wave function for TSC cluster:

$$\Psi_t = a_1 \Psi(1,1) + a_2 \Psi(2,2) + a_4 \Psi(4,4)$$

- Modal Fusion Rate:

$$\lambda = a_1^2 \lambda(1,1) + a_2^2 \lambda(2,2) + a_4^2 \lambda(4,4)$$

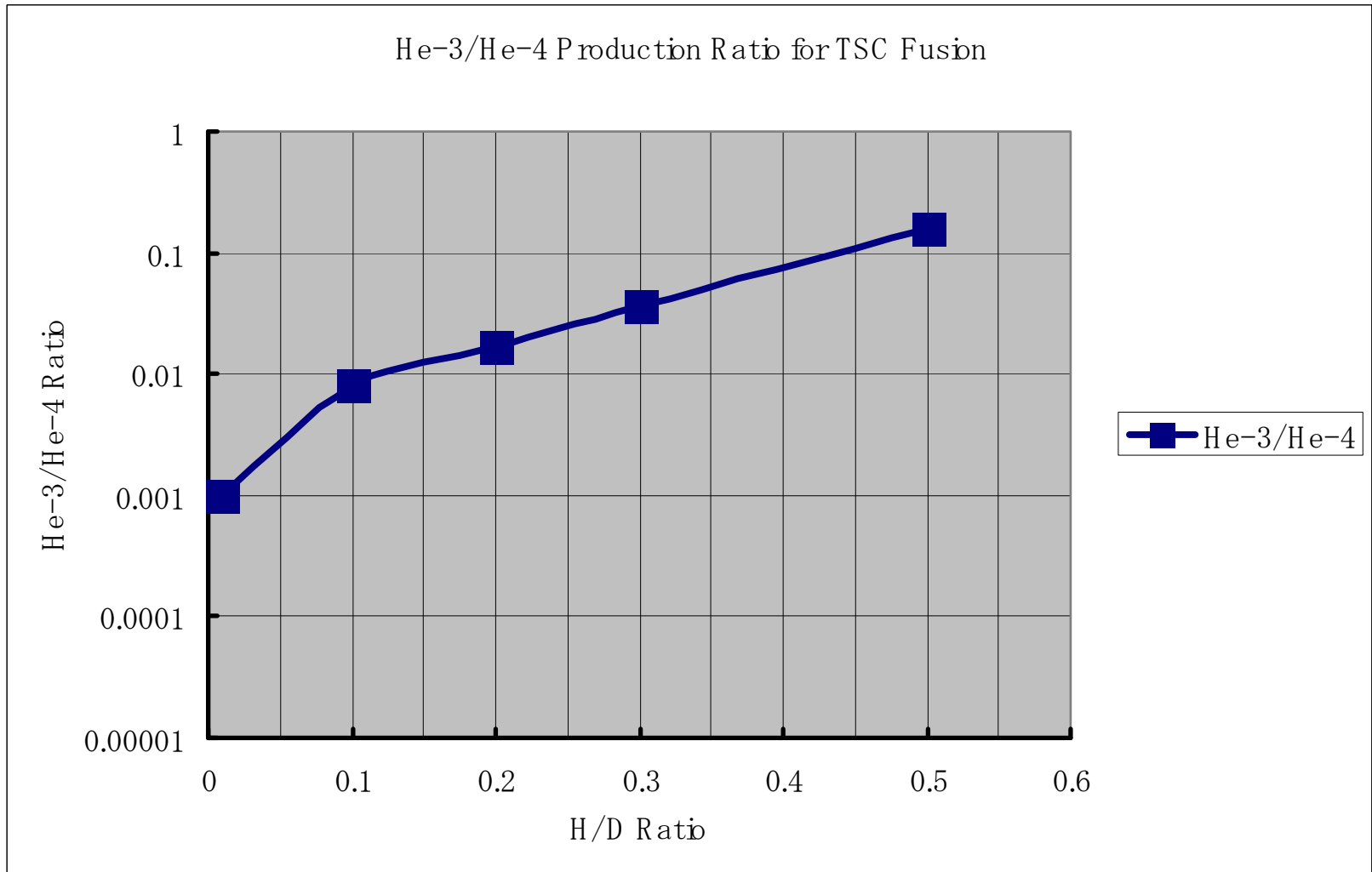
- By taking into account spin arrangement only, $a_1^2=0.78$, $a_2^2=0.19$, $a_4^2=0.03$

Modal Fusion Rate

- Considering statistical weights for spin arrangement, modal fusion rates were calculated using FRs of EQPET molecules

DDDD-TSC	DDDH-TSC	DHDH-TSC
$\lambda_{dd} = 2E-21$ (f/s/cl)	$\lambda_{dp} = 1E-23$ (f/s/cl)	$\lambda_{dp} = 1E-23$ (f/s/cl)
$\lambda_{dddd} = 3E-11$ (f/s/cl)	$\lambda_{dddp} = 4E-12$ (f/s/cl)	$\lambda_{dpdp} = 3E-12$ (f/s/cl)

Using combination probabilities of H/D mixed clusters and modal fusion rates, $^3\text{He}/^4\text{He}$ ratios were calculated



Comparison with Experiment

- Arata-Zhang; $^3\text{He}/^4\text{He}$ ca. 0.25
Proc. Jpn. Acad., 73, Ser.B(1997)1-7
- Present Theory;
 $^3\text{He}/^4\text{He}$ ca. 0.25 for $\text{H}/\text{D} = 0.6$

Parameters for Deep Potential Hole : by EQPET

• $(m^*/m_e : Z)$ • for e^*	depth of trapping potential (DTP)	
	dde*	dde*e*
• (1,1)	- 14.87 eV	- 30.98 eV
• (2,2)	- 260 eV	- 446 eV
• (4,4)	- 2,460 eV	- 2,950 eV
• (8,8)	- 21.0 keV	- 10.2 keV

•DTP values approximately correspond to Screening Energy

Emission of Photons from TSC

- Hydrogen TSC (pepepepe system) causes no nuclear fusion, but weak interaction.
- When TSC forms from normal electron state, we may have specific photon emission, e.g., at energies of 260 eV, 446 eV, 2460 eV, 2950 eV, etc.
- If we can detect these photons by hydrogen experiment, it may be proof.

Minimum Size of TSC is far less than 1 pm!

- 4d + 4e of TSC squeezes into a very small charge-neutral pseudo-particle.
- When 4d reach at the interaction range (several fm) of strong force, ${}^8\text{Be}^*$ is formed by QM-penetration through EQPET shielded potential.
- As ${}^8\text{Be}^*$ is formed, 4e are left at outer domain, which size is approximated by $e^*(4,4)\text{Be}$ atom size of 0.8 pm.

V_s Potential for $e^*(4,4) \alpha \alpha$ molecule

$$\text{min} = -9.83 \text{ keV}$$

$$\text{dd(GS)} = 13 \text{ pm}$$

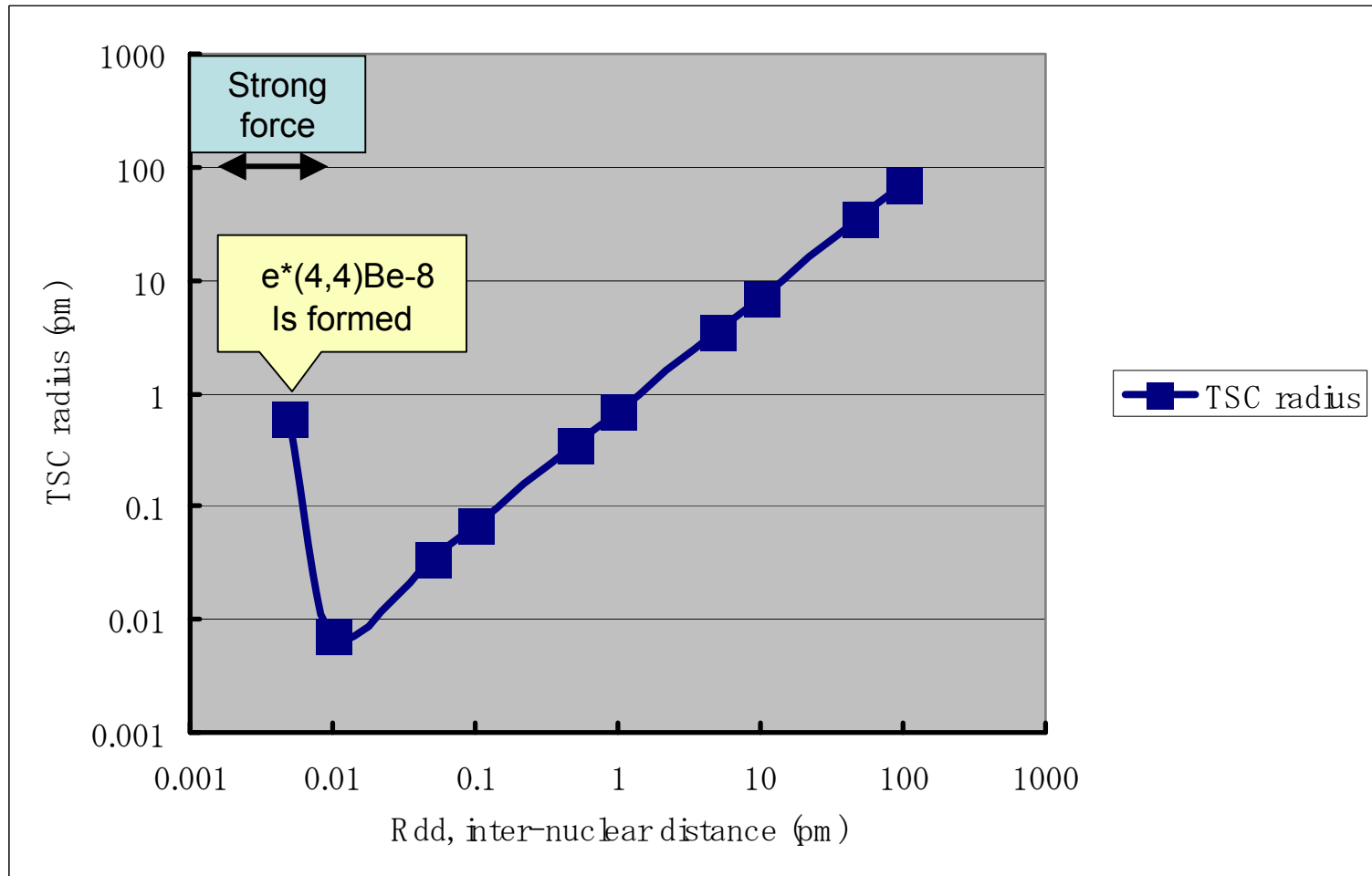
V_s Potential for $e^*(8,8)^8\text{Be}^8\text{Be}$ molecule

$$V_{\text{min}} = -32.9 \text{ keV}$$

$$R_{\text{dd(GS)}} = 5 \text{ pm}$$

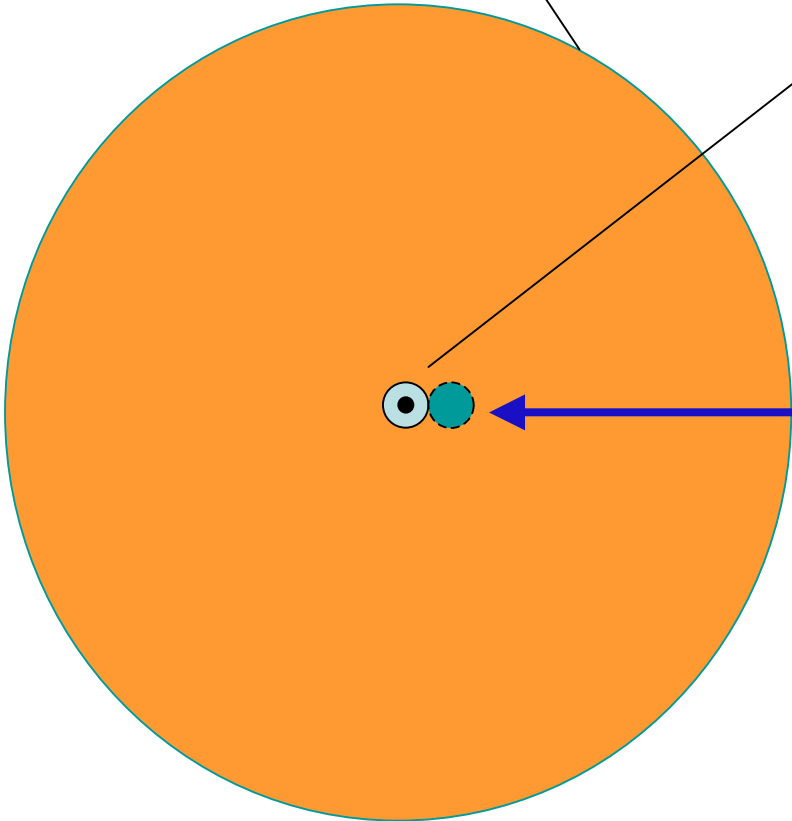
$$\text{b-parameter} = 60 \text{ fm (radius, OSC transient)}$$

TSC Size by Dynamic Condensation



Target Atom Outer Electron Cloud (ca. 100 pm)

K-Shell e⁻ And Nucleus



Neutral Pseudo-Particle

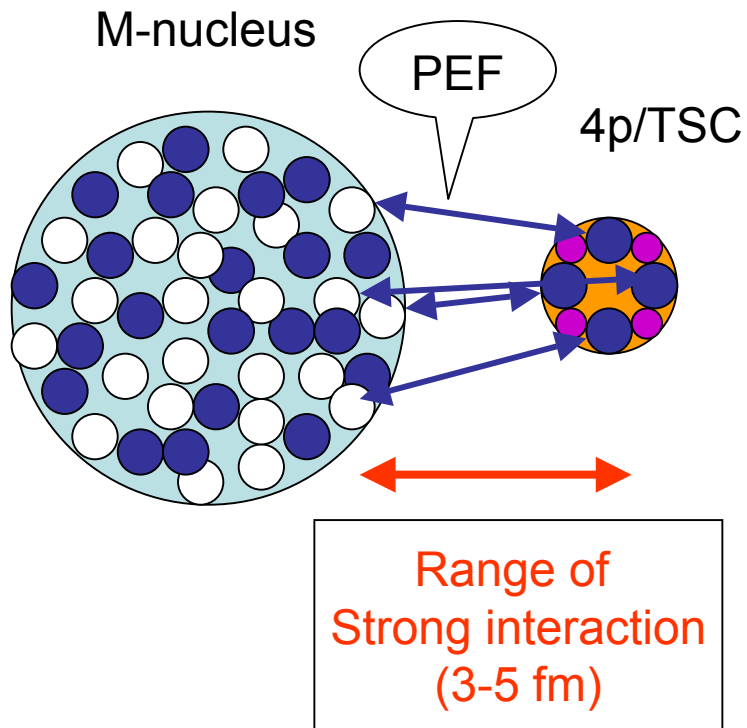
TSC, < 1 pm
(4P+4e): neutral



How deep can TSC penetrate through e-cloud?

M + TSC

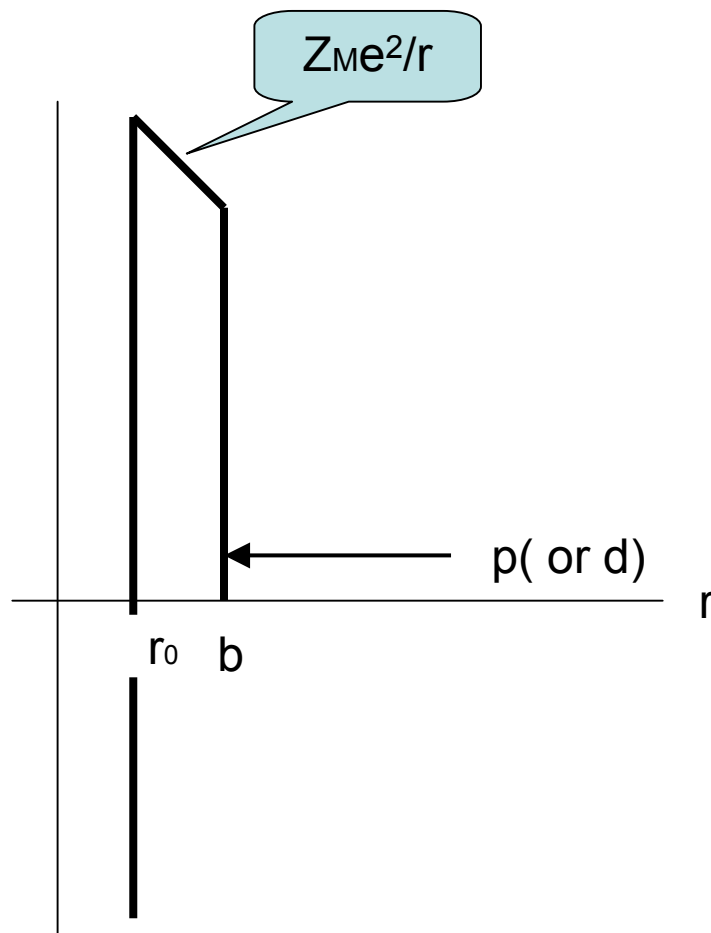
Nuclear Interaction Mechanism



- Topological condition for Pion-Exchange (PEF)
- Selection of pick-up number of protons (+ neutrons for 4d/TSC) from 4p/TSC
- $M + (1-4)p(\text{or } d)$ capture reaction

Sudden Tall Thin Barrier Approx.

When p (or d) gets into the strong force range, electrons separate and p (or d) feel suddenly Coulomb repulsion to the M -nucleus charge



- $r_0 = 1.2A^{1/3}$
- $b = r_0 + \lambda_\pi (=2.2 \text{ fm})$
- $P_M(E) = \exp(-G)$
- $G = 0.436(\mu V(R_{1/2}))^{1/2}(b - r_0)$
- $R_{1/2} = r_0 + (b - r_0)/2$
- Reaction rate:

$$\lambda = S_{Mp}(E)vP_M(E)P_n/E$$
- $P_n =$

$$\exp(-0.218n(\mu V_{pp})^{1/2}R_{pp})$$

: Plural p (or d) existence probability in λ_π range for $n > 1$. $P_n = 1$, for $n = 1$.

Results by STTBA calculation; M = Ni

- $P_{Mp}(E) = 9.2E-2$
- $P_{Md}(E) = 3.5E-2$

Reaction Rates:

- $\lambda_{Mp} = 3.7E-8$ (f/s/pair)
- $\lambda_{Md} = 2.1E-7$ (f/s/pair)
- $\lambda_{M4p} = 1.0E-8$ (f/s/pair)
- $\lambda_{M4d} = 3.4E-9$ (f/s/pair)

- $\langle \text{Macroscopic Reaction Rate} \rangle = \lambda x N_{M+TSC}$

- With $N_{M+tsc} = 1.0E+17$ in $10\mu\text{m}$ area, Ni+4p Rate = $1E+9$ f/s/cm² and $Y_{4p} = 1E+15$ in $1E+6$ sec.
- 1 watt = $2E+11$ f/s, and $1E+9$ f/s/cm² is **5 mW/cm²**

$$V_{pp} = 1.44/6 = 0.24 \text{ MeV}$$

$$P_{2p} = 0.527$$

$$P_{2d} = 0.404$$

$$S_{Mp}(0) = 1.0E+8 \text{ kevb}$$

$$S_{Md}(0) = 1.0E+9 \text{ keVb}$$

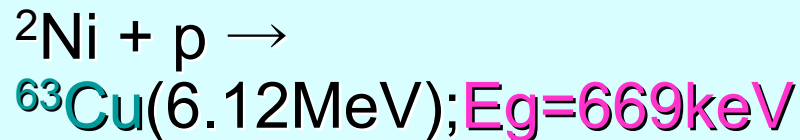
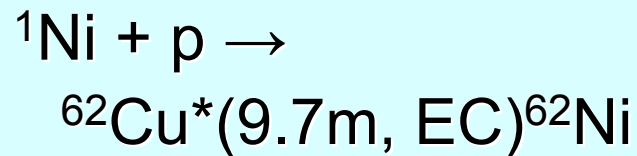
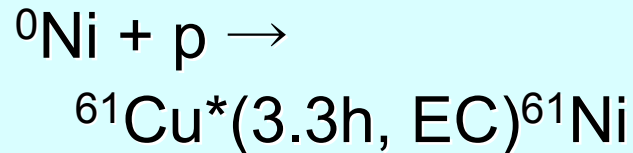
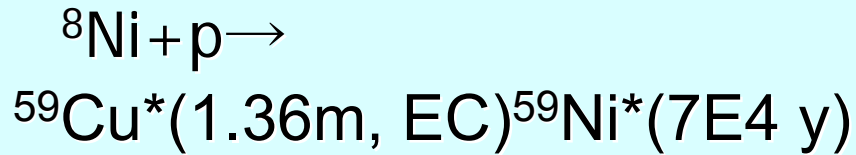
$$\lambda_{4d} = 4.9E-5$$

Estimation of N_{M+TSC}

- $N_{M+TSC} = \sigma_A N_M \langle N_{TSC} \rangle v T_{TSC}$
- N_M : Host metal atom density
- N_{TSC} : Time-averaged TSC density
- σ_A : Atomic level cross section for M+TSC combination
- T_{TSC} : mean life time of TSC
- Note: approximated by the squeezing time of TSC from 1 angstrom domain to 5 fm domain, because strong interaction breaks TSC.

- $\tau_{TSC} = 45$ fs (for p),
66 fs
(for d)
- $\sigma_A = 1E-16$ (cm²)
- $N_M = 1E+23$ (cm⁻³)
- $N_{TSC} = 1E+20$ (cm⁻³)
is assumed here
- $N_{M+TSC} = 1E+19$ (cm⁻³)

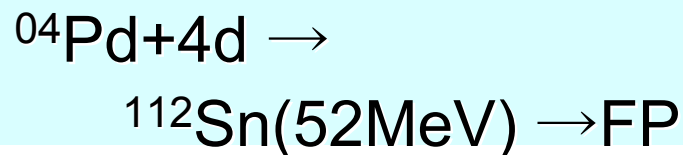
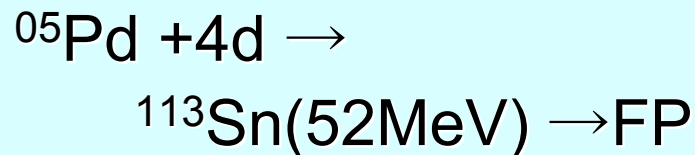
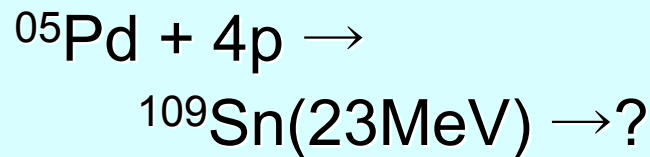
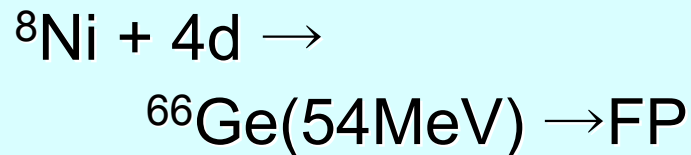
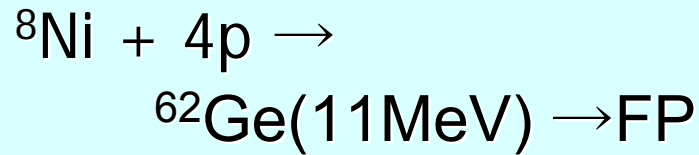
Products by Ni + p reactions



**i-H gas system exp.
By Piantelli (ASTI5)
; 660 keV peak by NaI
detector**

- 660 MJ Excess Energy

Fission by M + TSC is possible!



any foreign elements
were detected by
Piantelli, Karabut,
Yamada, Ohmori,
Mizuno, Miley, etc.

fission can be induced by
TSC capture!

^{133}Cs + TSC Reactions

- $^{133}\text{Cs} + d \rightarrow ^{135}\text{Ba}(\text{Ex}=12.91\text{MeV}) \rightarrow$
 $^{135}\text{Ba}(\text{stable}) + \text{gammas}(12.91\text{MeV})$
- $^{133}\text{Cs} + 2d \rightarrow ^{137}\text{La}(\text{Ex}=25.32\text{MeV}) \rightarrow \text{FPs}$
or $^{137}\text{La}(6\text{E}+4 \text{ y}) + \text{gammas}$
- $^{133}\text{Cs} + 3d \rightarrow ^{139}\text{Ce}(\text{Ex}=38.29\text{MeV}) \rightarrow \text{FPs}$
or $^{139}\text{La}(\text{stable}) + \text{gammas}$
- $^{133}\text{Cs} + 4d \rightarrow ^{141}\text{Pr}(\text{Ex}=50.49\text{MeV}) \rightarrow \text{FPs}$
or $^{141}\text{Pr}(\text{stable}) + \text{gammas}$

Note: (1) + 2d is equivalent to $^4\text{He} + 23.8\text{MeV}$.

(2) We need to detect 50.49 MeV gamma?

M+4d/TSC is much easier than M+4p

- Because fusion strong force (PEF values) for M+4d is about twice of M+4p
- (c.f.) $S_{dd}/S_{pd} = 10^6$
with PEF = 2 for dd
and PEF = 1 for pd
- Because we need to multiply probability of anti-parallel spin arrangement for protons in 4p-TSC.

- $^{133}\text{Cs}+p \rightarrow ^{134}\text{Ba}(8.17\text{MeV})$
 $\rightarrow ^{134}\text{Ba}(\text{stable})$
- $^{133}\text{Cs}+2p \rightarrow ^{135}\text{La}(13.16\text{MeV})$
 $\rightarrow ^{135}\text{Ba}(\text{stable})$
- $^{133}\text{Cs}+3p \rightarrow ^{136}\text{Ce}(20.28\text{MeV})$
 $\rightarrow ^{136}\text{Ce}(\text{stable})$
or FPs
- $^{133}\text{Cs}+4p \rightarrow$
 $^{137}\text{Pr}(24.28\text{MeV}, 1.28\text{d})$
 $\rightarrow ^{137}\text{Ce}(1.43\text{d})^{137}\text{La}$
or FPs

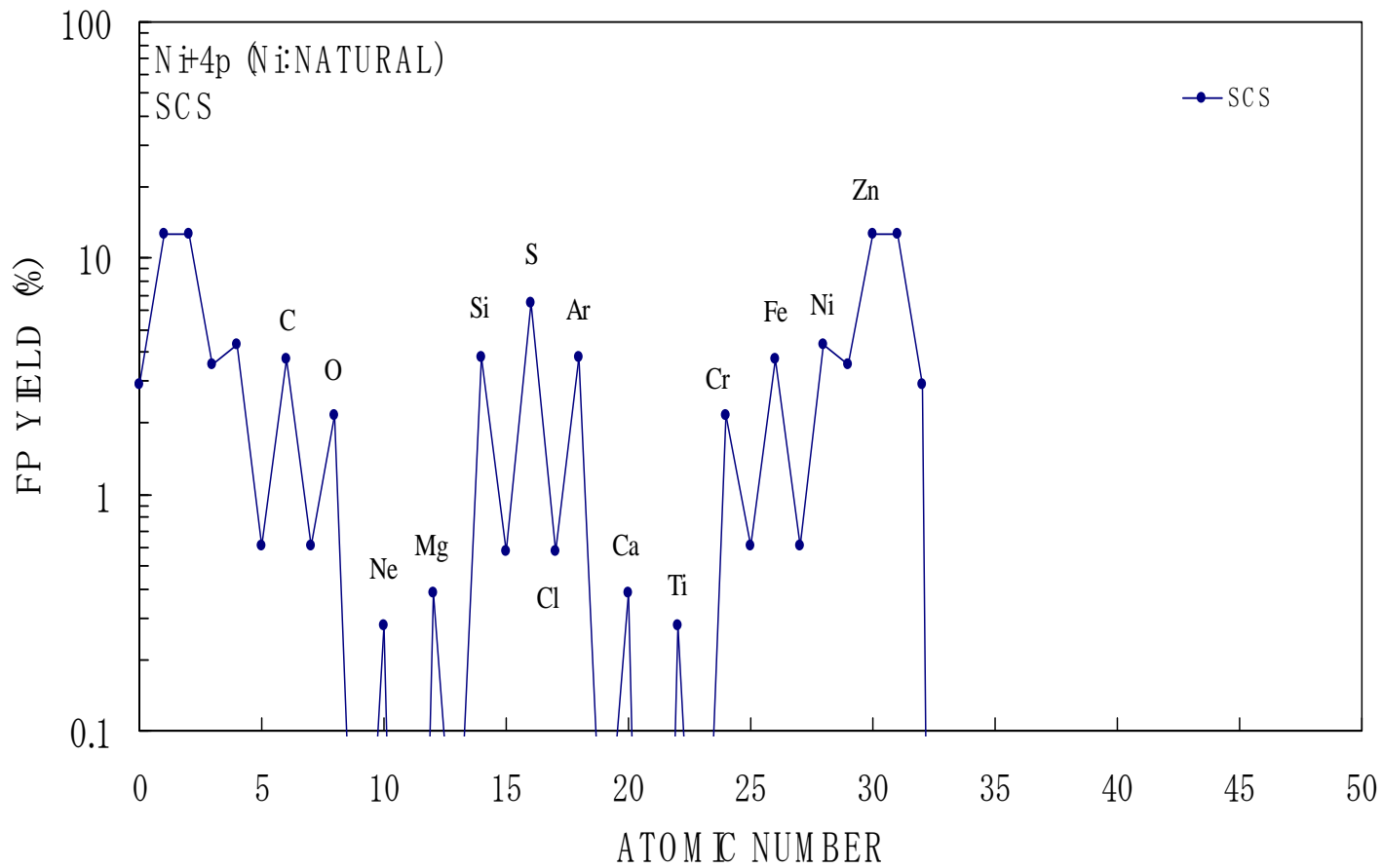
STTBA Prediction for Cs-to-Pr

- $S_{Mp} = 1E+8$ kevb
- $S_{Md} = 1E+9$ keVb
- $\lambda_{Mp} = 8.4E-10$ f/s/pair
- $\lambda_{M4p} = 2.3E-10$ f/s/pair
- $\lambda_{Md} = 2.8E-8$ f/s/pair
- $\lambda_{M4d} = 7.6E-9$ f/s/pair
- Where combination probability of anti-parallel spin was used for 4p/TSC.

- Suppose $N_{M+tsc} = 1E+17$ in 100 nm layer of surface
- Macro Yield = $\lambda \times N_{tsc} = (7.6E-9) \times (1E+17)$
= $7.6E+8$ (f/s/cm²)
- Cs-to-Pr rate =
 $4.6E+14$ (atoms per week)
per cm²
- Here we assumed;
 $\langle N_{Tsc} \rangle = 1E+22$ (cm⁻³), due to high D₂-flux condition in experiment

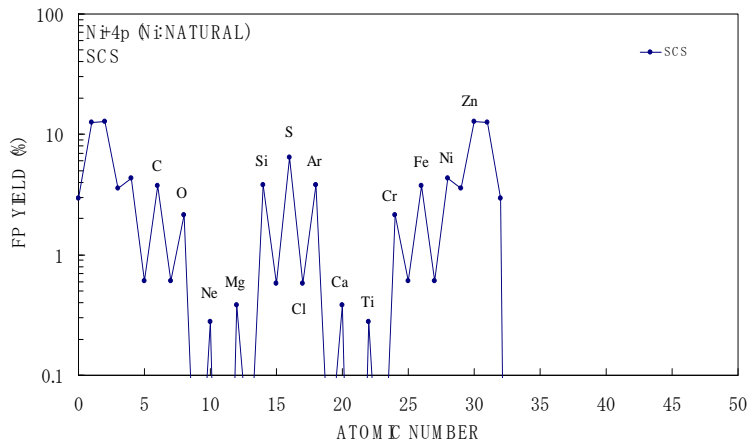
Table : Natural abundance of Ni isotopes and
the excitation energies of compound nucleus by + 4p and + 4d reactions

Nuclides	Natural abundance (%)	+ 4p	Excitation energy (MeV)	+ 4d	Excitation energy (MeV)
^{58}Ni	68.077	$^{62}\text{Ge}^*$	11.2	$^{66}\text{Ge}^*$	53.9
^{60}Ni	26.223	$^{64}\text{Ge}^*$	19.1	$^{68}\text{Ge}^*$	55.1
^{61}Ni	1.140	$^{65}\text{Ge}^*$	21.3	$^{69}\text{Ge}^*$	55.4
^{62}Ni	3.634	$^{66}\text{Ge}^*$	24.0	$^{70}\text{Ge}^*$	56.4
^{64}Ni	0.926	$^{68}\text{Ge}^*$	29.0	$^{72}\text{Ge}^*$	58.0

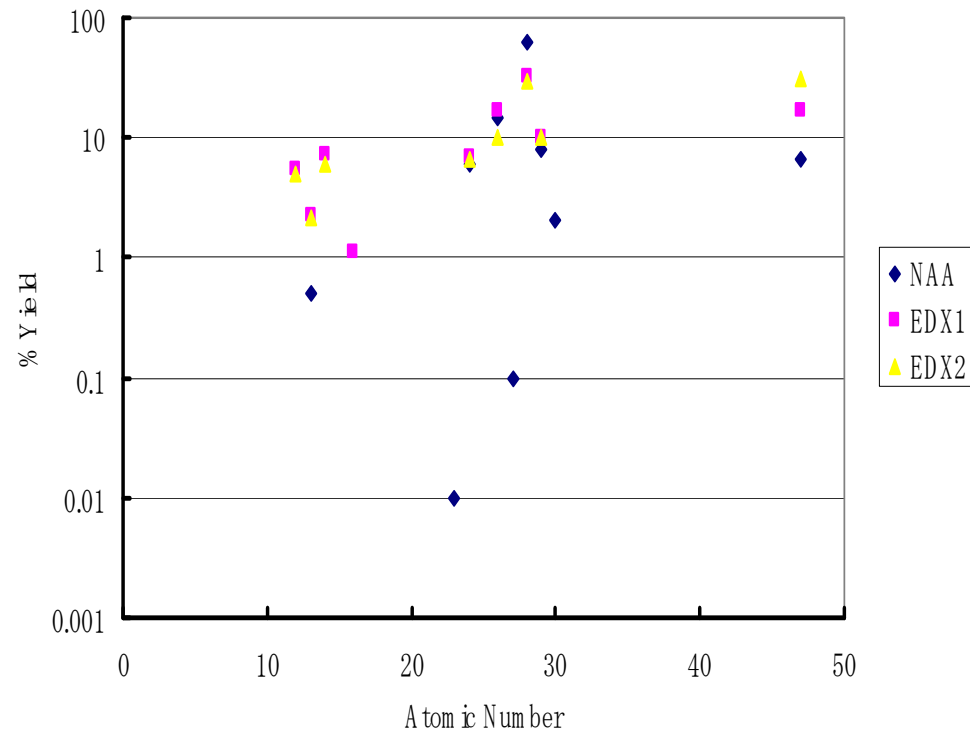


FP Elements by SCS vs. Miley Exp.

G. Miley and J. Patterson
 J. New Energy, 1996, 1, p.5

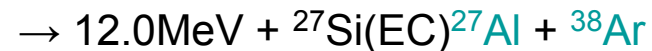
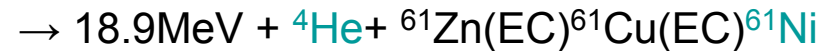
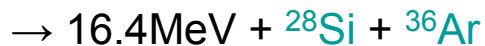
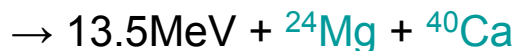
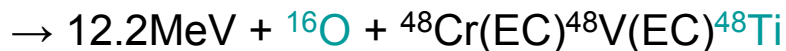
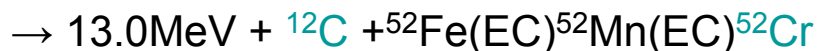
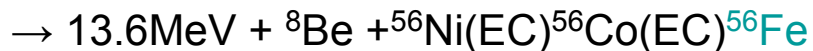
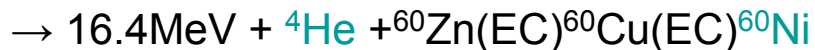
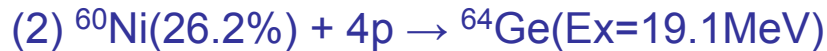
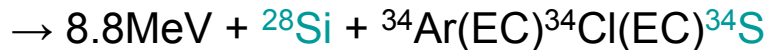
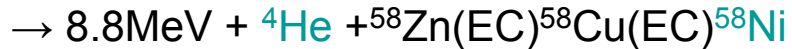


Data from Miley '96



Ni + 4p/TSC to fission
 Calculated by
 Selective Channel Fission Model

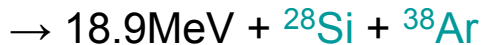
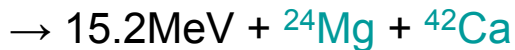
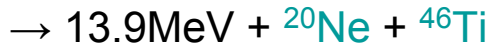
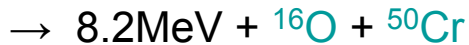
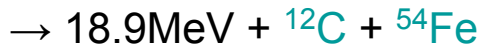
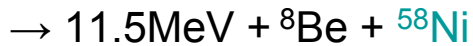
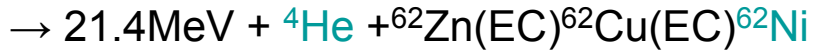
Major Fission Channels from Ni + 4p



Note:

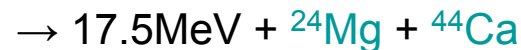
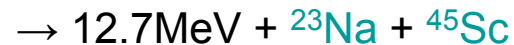
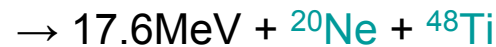
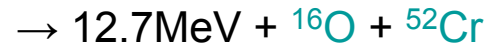
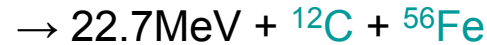
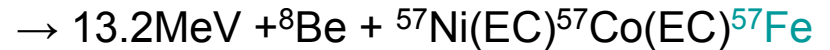
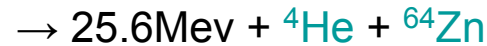
- Green shows stable isotope.
- Average Kinetic Energy of Fission Product = 9.7 MeV for Ni-natural

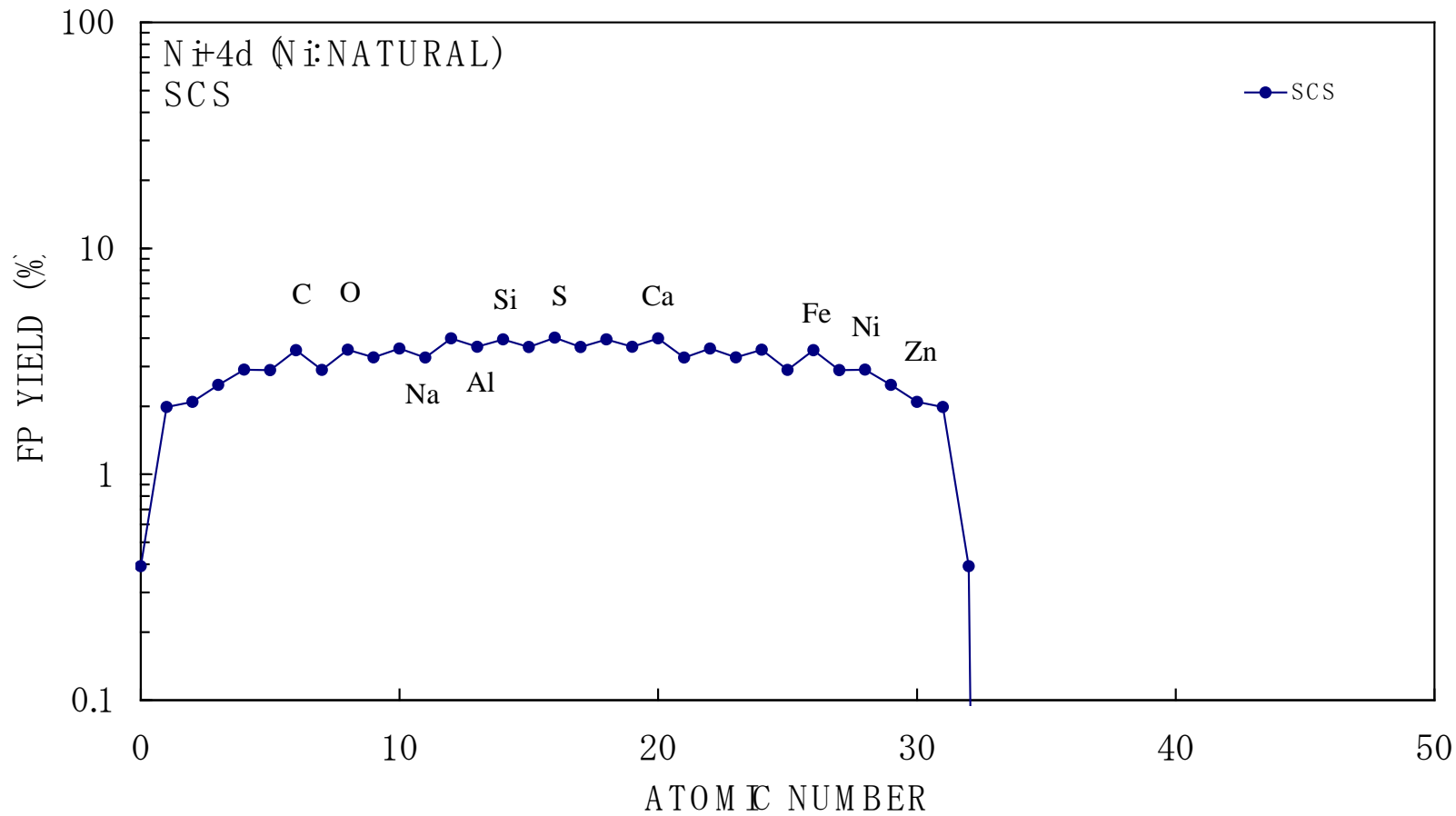
Major Fission Channels from Ni + 4p (2)



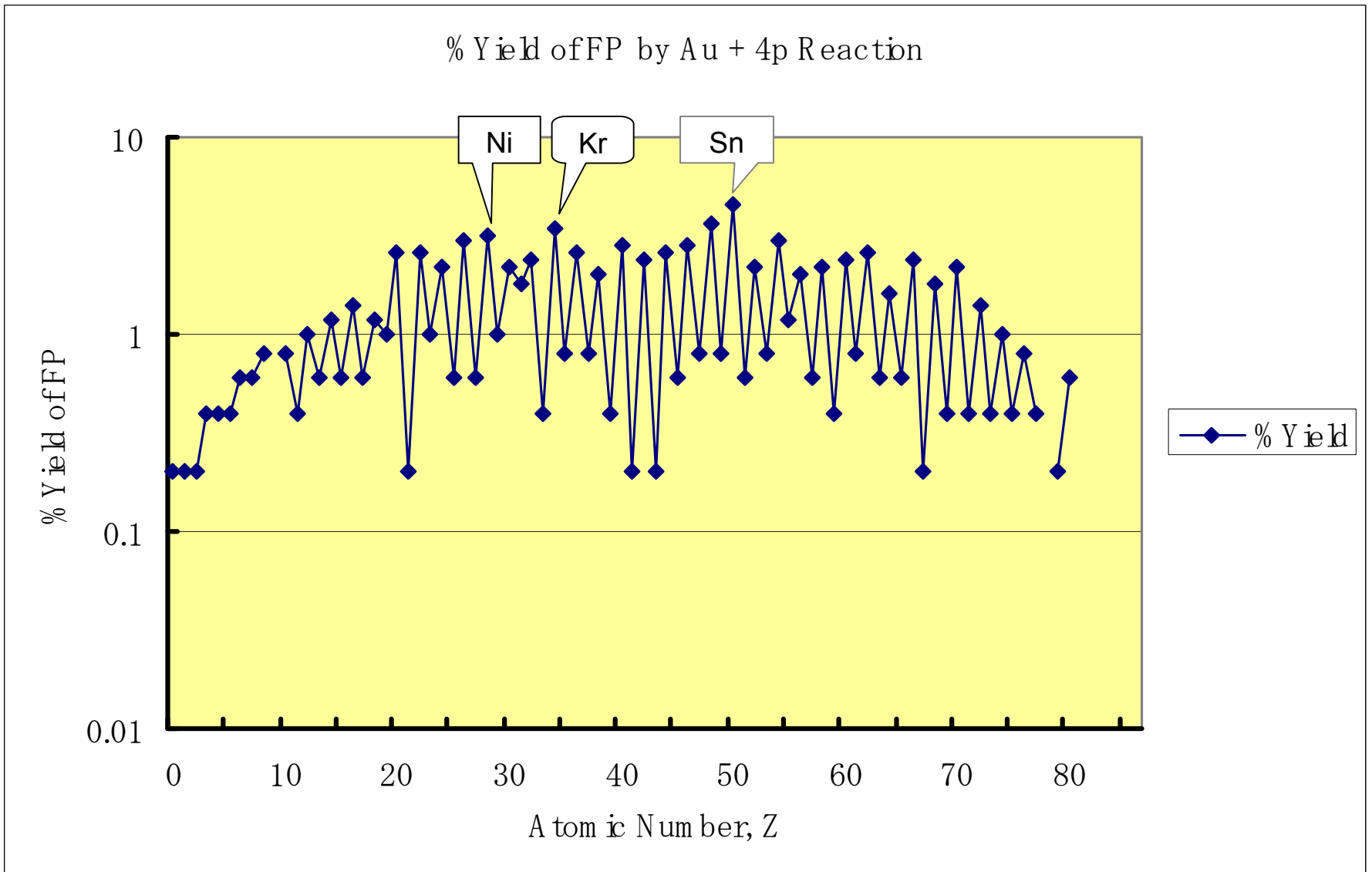
- Neutron emission channel may open!

- S-values for higher mass Ni may be larger than Ni-58 and Ni-60, due to more p-n PEF interaction.





FP Distribution vs. Z, for Au + 4p/TSC



Secondary Reactions by ^3He

- ^3He by D+D+D+H fusion has 16.7 MeV, and by D+H+D+H fusion 5.5 MeV.
- Coulomb Barriers:
Cs + ^3He : 15.7 MeV
Pd + ^3He : 14.1 MeV
- Small reaction is predicted by 16.7 MeV ^3He during its slowing down,
- and nothing by 5.5 MeV ^3He .

^3He for Stable Nuclear Fuel

- Stable Resource to produce Tritium:
 $^3\text{He} + n \rightarrow p + t + 0.765 \text{ MeV}$: in fission reactor or spallation source. Easy to extract T from gas-phase.

Tritium decays with 12.3 yrs half life.

For DT reactors and H-bomb.

(neutron detector)

- Fuel for D- ^3He reactors.

Conclusions

- H should be contained with some amount in usual CMNS deuterium-experiment.
- EQPET model was applied to 4-body fusion of mixed H/D TSC-system.
- ${}^3\text{He}/{}^4\text{He}$ production ratio was 0.16 for 50 % H-contamination.
- ${}^3\text{He}$ is useful nuclear fuel.
- Formation of TSC is Key!
- Possibility of direct nuclear reaction for M+TSC. (Further study is expected.)