

# Hydrogen-lithium Low Energy Resonant Electron-Capture and Bethe's Solar Energy Model

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## Content:

**1. 3-parameter formula**

Who participate the reaction ?

**2. Selective Resonance Tunneling**

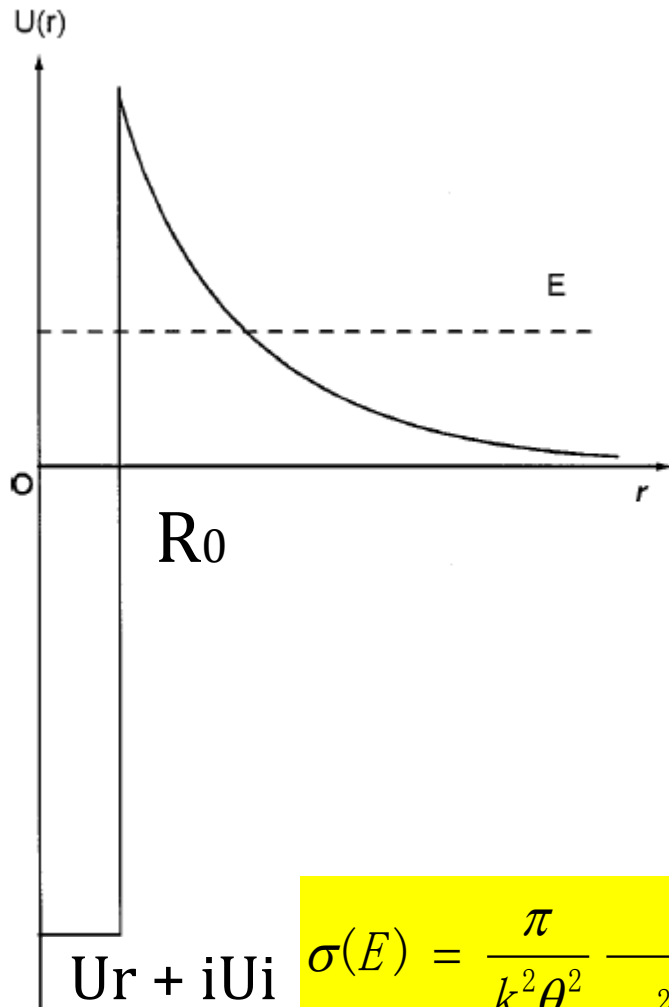


How the reaction happen?

**3. Bethe's Solar Model**

What's reaction probability ?

# 1. 3-parameter formula for fusion cross-section of light nucleus



3 parameters for light nucleus fusion model (non-elastic scattering):

$R_0$ : the radius of target nucleus

$U_r$ : the depth of nuclear potential well

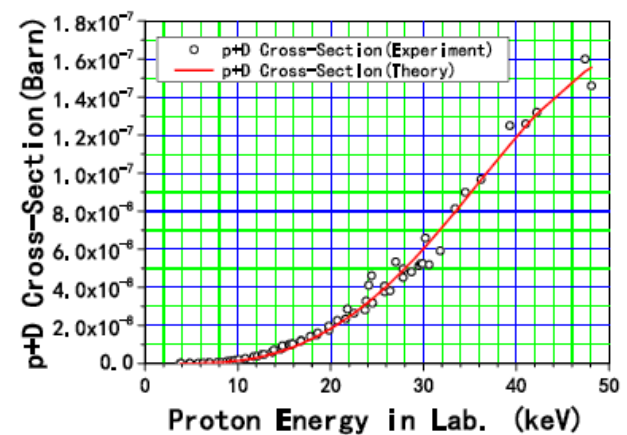
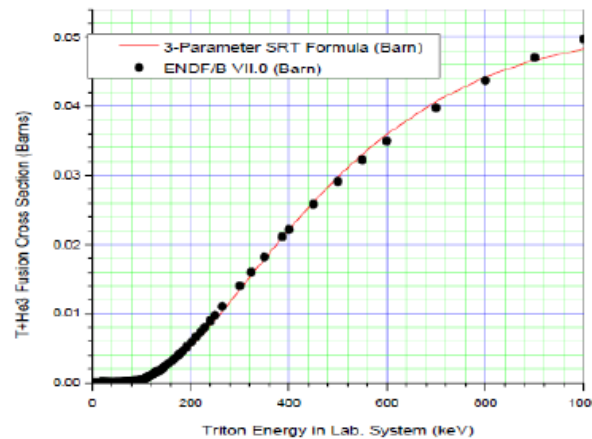
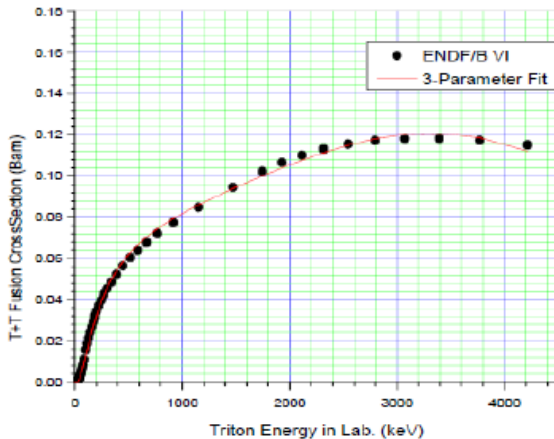
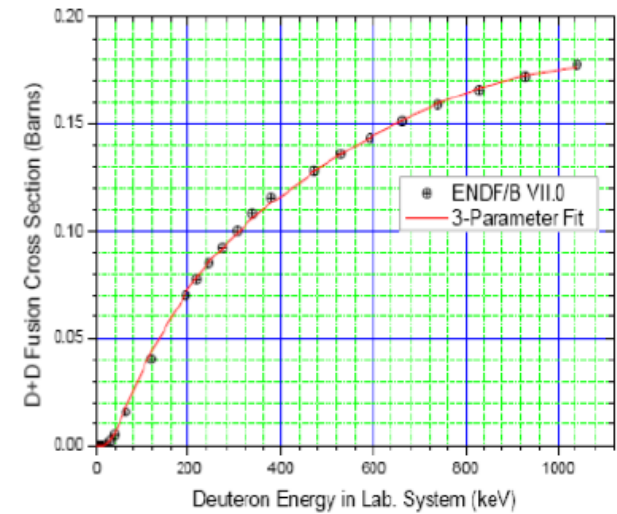
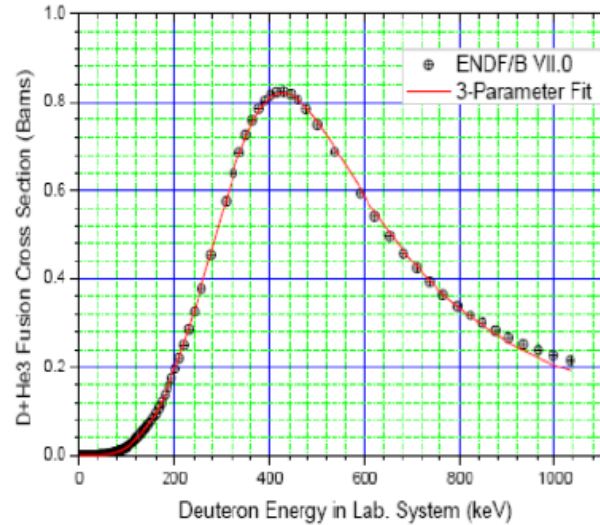
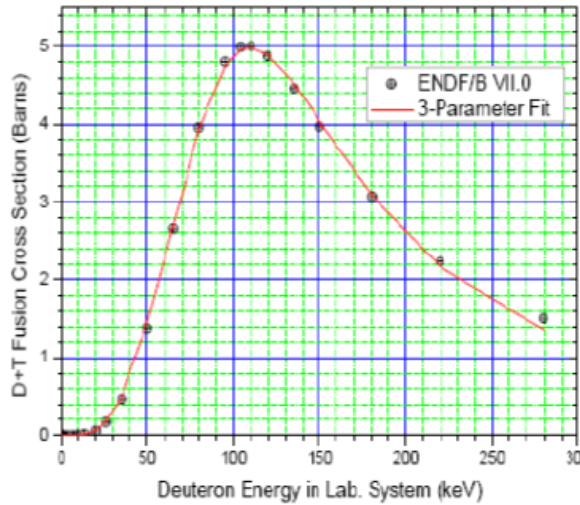
$U_i$ : the imaginary part of nuclear potential well (describes the absorption of the well)



$C_1, C_2, w_i$

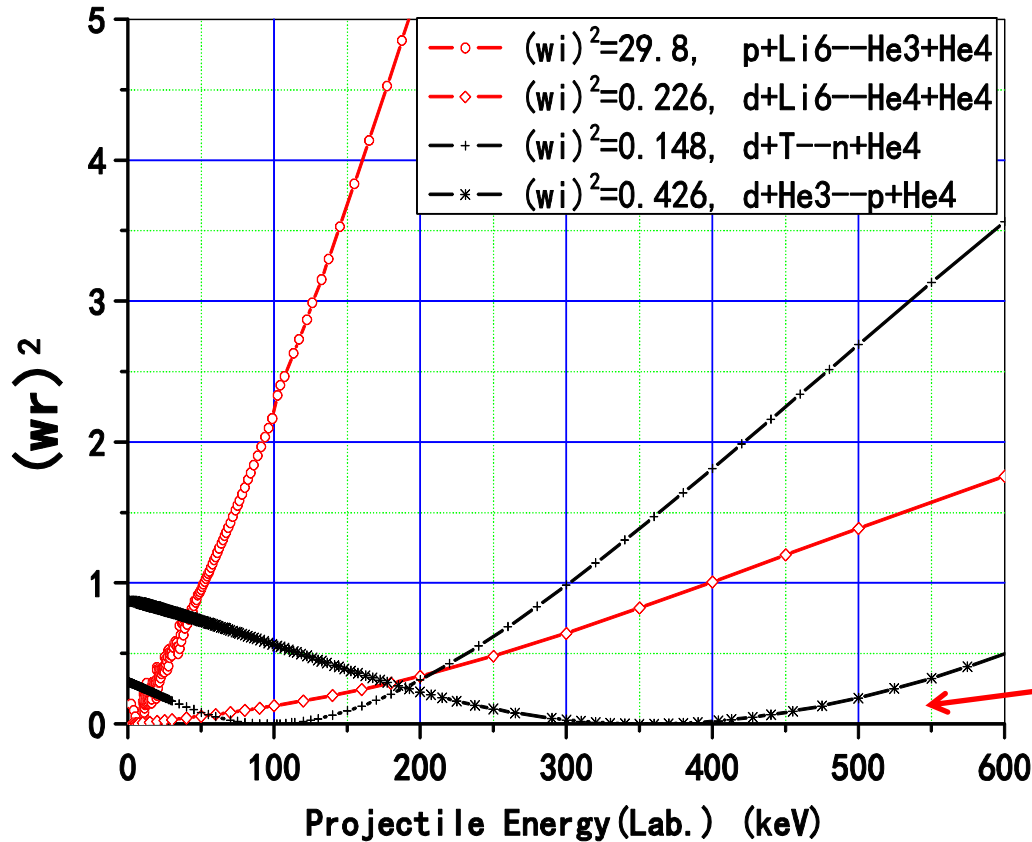
$$\sigma(E) = \frac{\pi}{k^2 \theta^2} \frac{-4w_i}{w_r^2 + \left(w_i + \frac{1}{\theta^2}\right)^2} \approx \frac{\pi}{k^2 \theta^2} \frac{-4w_i}{(C_1 + C_2 E)^2 + \left(w_i + \frac{1}{\theta^2}\right)^2}$$

# 1. 3-parameter formula for fusion cross-section of light nucleus



3-parameter formula was supported by hot fusion data:  
D+T, D+He3, D+D, T+T, T+ <sup>3</sup>He, p+D, etc

# 1. 3-parameter formula for fusion cross-section of light nucleus



$$\sigma(E) = \frac{\pi}{k^2 \theta^2} \frac{-4W_i}{W_r^2 + (W_i - 1/\theta^2)^2}$$

$$W_r^2 = \frac{\pi}{k^2} \frac{(-4W_i)}{\theta[E]^2 \sigma_0[E]} - \left(W_i - \frac{1}{\theta[E]^2}\right)^2$$

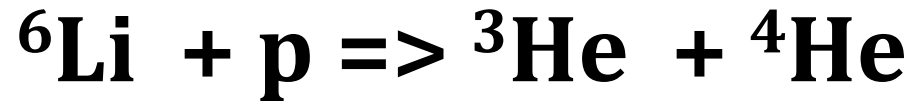
d+T resonance at 95keV, d+<sup>3</sup>He resonance at 375keV

- describes resonance
- **p + <sup>6</sup>Li**, and **d + <sup>6</sup>Li** resonance at **E~0**

## 2. Selective Resonant Tunneling



Can we expect



At  $E \sim 0$  ?

**No!**

## 2. Selective Resonant Tunneling

$$\sigma(E) = \frac{\pi}{k^2 \theta^2} \frac{-4w_i}{w_r^2 + (w_i + 1/\theta^2)^2}$$

At resonance  
 $w_r = 0$ ,

$$\sigma(E) = \frac{\pi}{k^2 \theta^2} \frac{4}{(-w_i)}$$

$w_i$  represent  
absorption  
of nuclear  
well

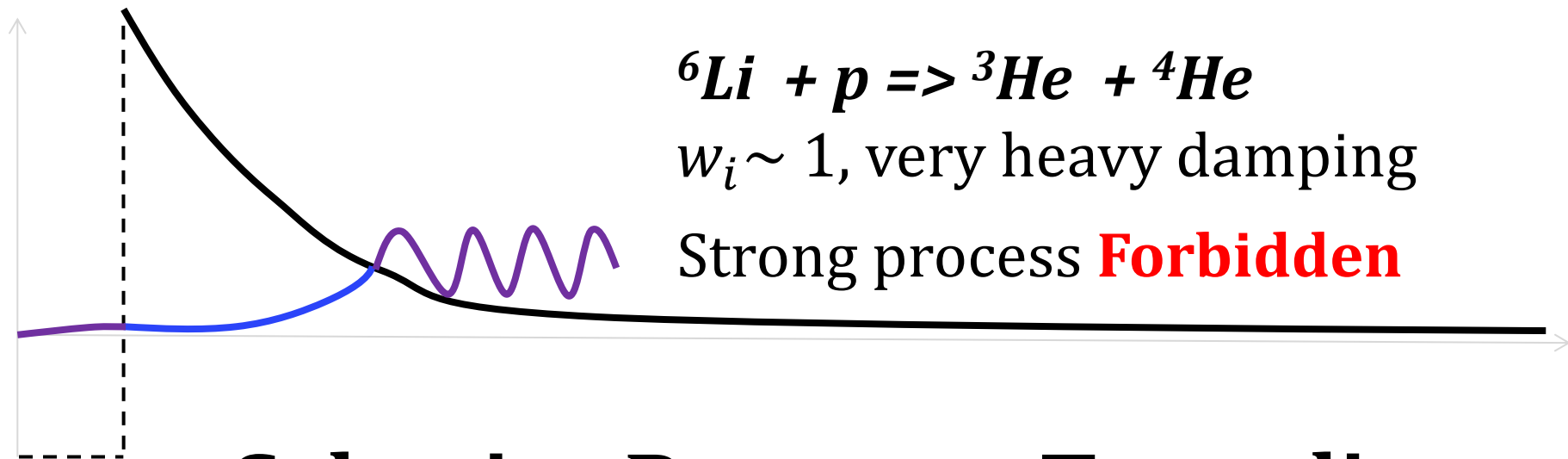
- $\theta^2 \approx \frac{1}{2\pi} \text{Exp} \left( \frac{Z_a Z_b e^2}{2\epsilon_0} \sqrt{\frac{m}{E}} \right)$  is Gamow factor, that is an extreme large number ( $> 10^{30}$ ) at low Energy.

• Strong interaction  $\Rightarrow -w_i \sim 1$

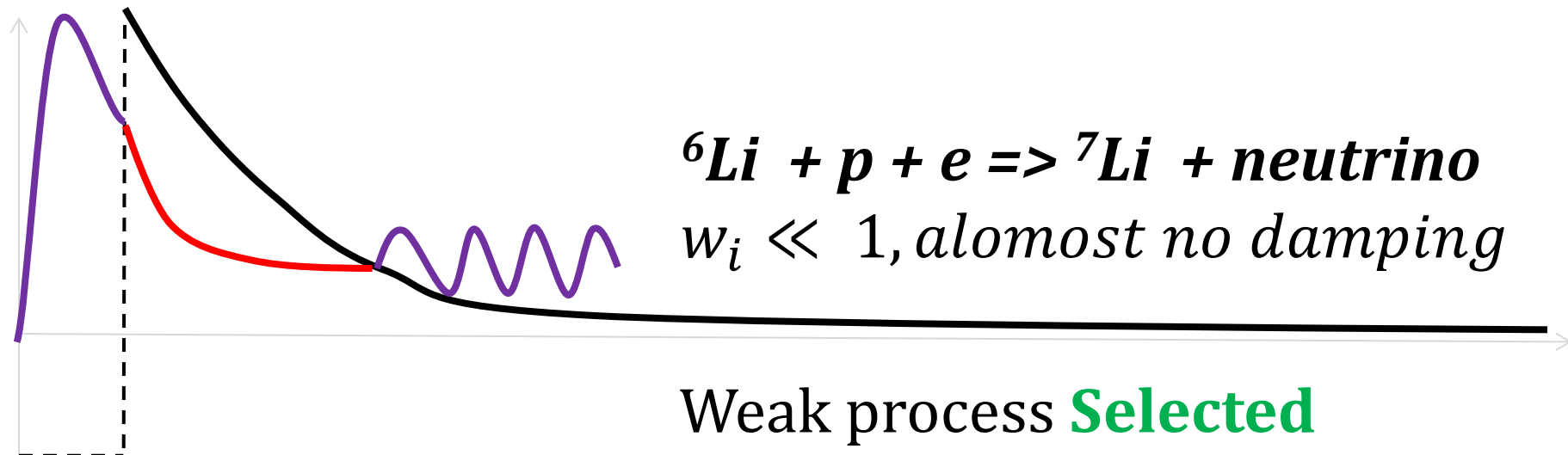
• Weak interaction  $\Rightarrow -w_i \sim 10^{-30}$

Only weak  
interaction  
will happen

## 2. Selective Resonant Tunneling



## Selective Resonant Tunneling





# Next Questions:

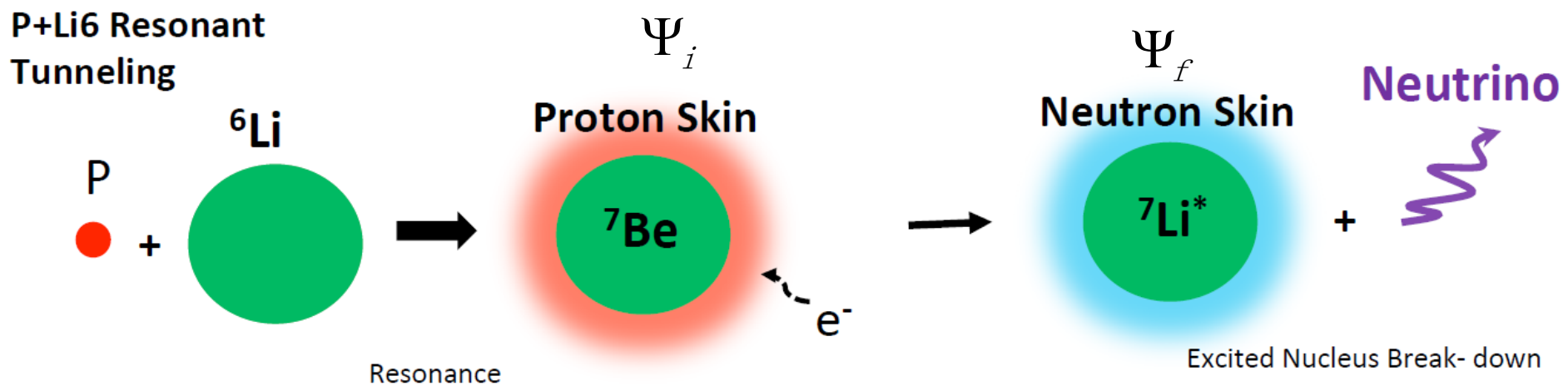
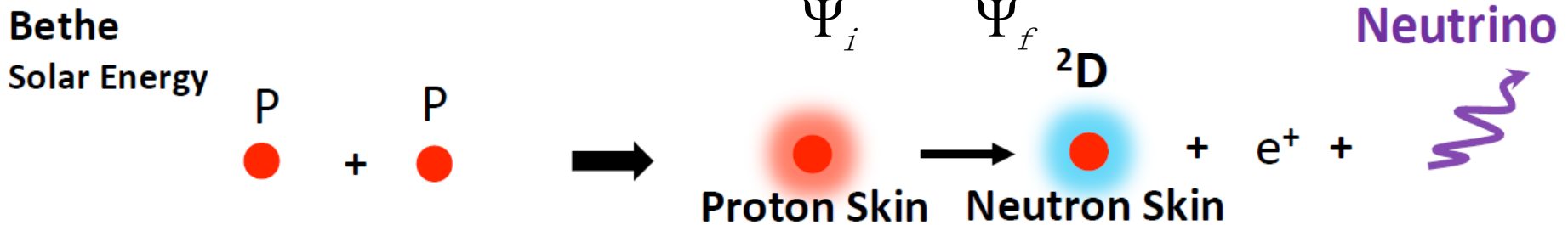
1. What's the energy width of the resonance?  
Does the energy width go to zero at  $E \sim 0$ ?
2. Imaginary potential well can't describe weak interaction. How to calculate the probability?



Method in **Bethe's Solar Energy model**

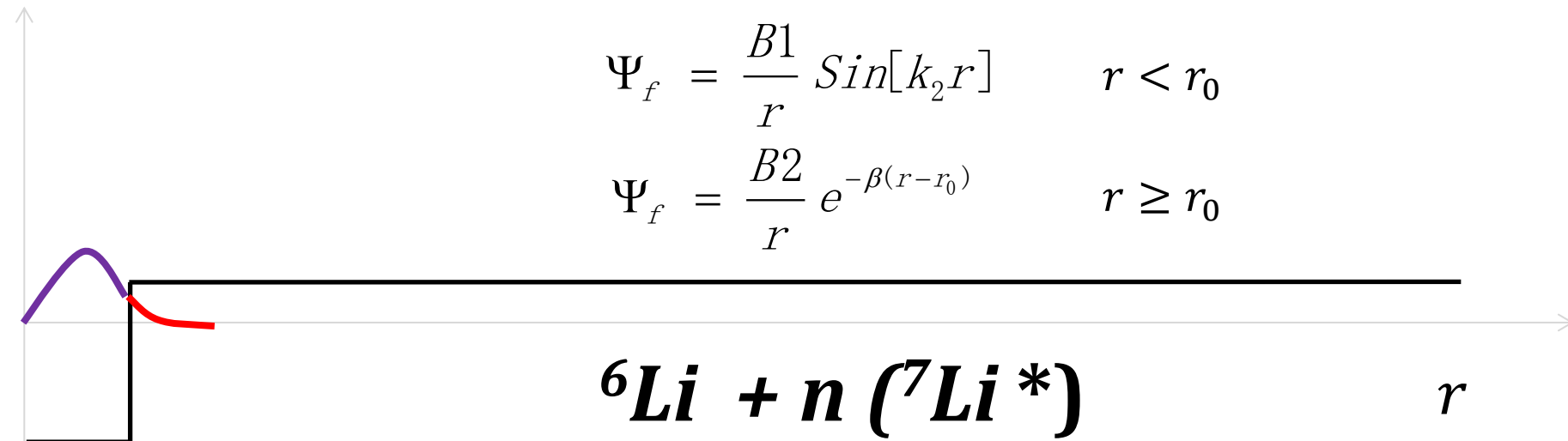
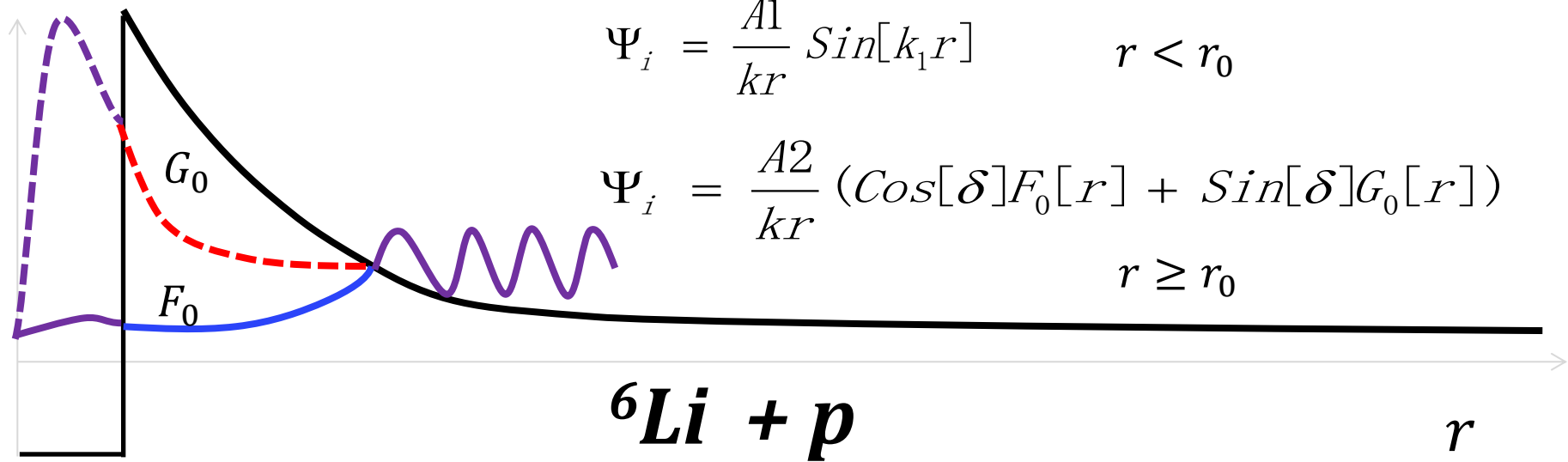
# 3. Bethe's Solar Energy Model

## Elastic Scattering--Weak Interaction



$$\sigma(E) = \frac{gF(W)}{v} \left| \int \Psi_f \Psi_i d\tau \right|^2$$

### 3. Bethe's Solar Energy Model



### 3. Bethe's Solar Energy Model



Reaction cross section from  $\Psi_i$  to  $\Psi_f$  is (in unit of  $m^2$ ):

$$\sigma(E) = \frac{gF(W)}{v} \left| \int \Psi_f \Psi_i d\tau \right|^2$$

At temperature  $T$ , average over Maxwell distribution, the reaction probability as below (in unit of  $m^3/\text{sec}$ ):

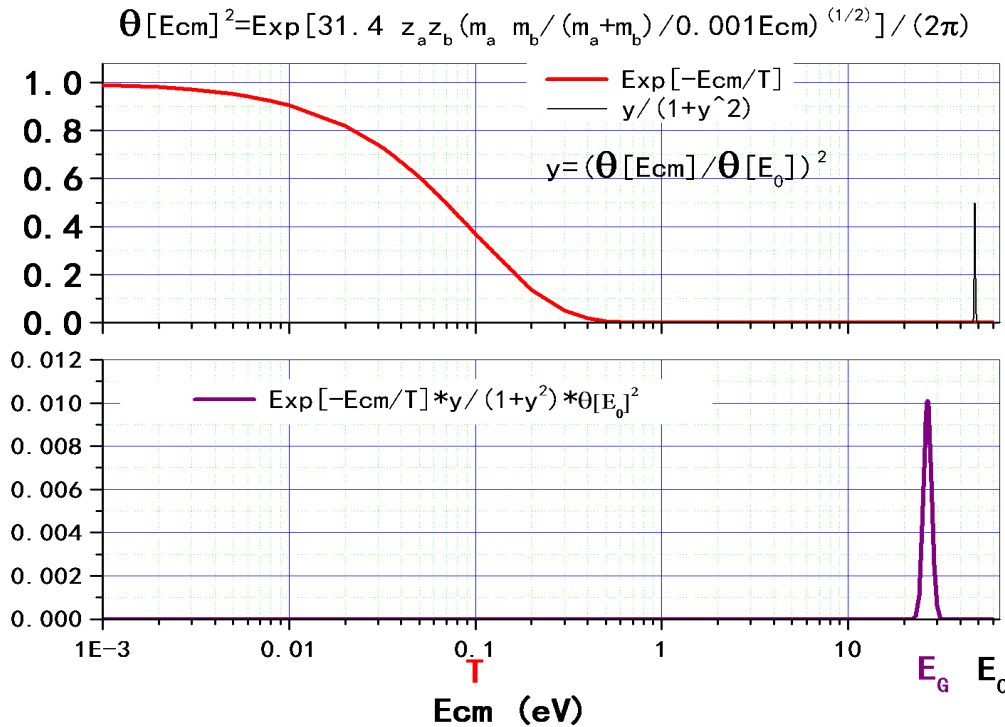
$$\langle \sigma[E] v \rangle = \left( \frac{\mu}{2\pi T} \right)^{3/2} \int_0^\infty gF(W) \left| \int \Psi_f \Psi_i d\tau \right|^2 \text{Exp}\left[-\frac{\mu v^2}{2T}\right] 4\pi v^2 dv$$

# 3. Bethe's Solar Energy Model



Resonance peak and resonance width:

$$\langle \sigma[E] v \rangle = C(T) (w_r)^2 \int_0^\infty \frac{\theta[E]^2}{1 + (w_r \theta[E]^2)^2} \text{Exp}\left[-\frac{E}{T}\right] dE$$



$$\theta[E_0]^2 w_r = 1$$

$$E_G = \left( \frac{\pi \hbar T}{\sqrt{2 \mu a_c}} \right)^{2/3}$$

$$\Delta E = 2 \sqrt{\frac{2 \text{Log}[2]}{|f'''[E_G]|}}$$

### 3. Bethe's Solar Energy Model



We assume  $E_0 = 50eV^*$  And  $T = 1300 k$

$$\frac{1}{W_r} = \theta[E_0]^2$$

$$E_G = \left( \frac{\pi \hbar T}{\sqrt{2\mu a_c}} \right)^{2/3} = 28.4eV$$

$$\Delta E = 2 \sqrt{\frac{2 \text{Log}[2]}{|f''[E_G]|}} = 3.4eV$$

It is a very broad way to proton tunneling !

\* In Lipinski's patent, he claimed that he was able to detect the helium when a low energy (50eV) proton beam was injected into the lithium vapor.

### 3. Bethe's Solar Energy Model



Reaction probability and Temperature dependence:

With parameters of  ${}^6\text{Li}$  and  $p$ , and assumed  $E_0 = 50\text{eV}$ , the reaction probability as below:

$A$  is independent with  $T$ , and  $T$  in Kelvin

$$\langle \sigma v \rangle = A \cdot \left(\frac{1}{T}\right)^{2/3} \cdot \text{Exp}\left[-\frac{8416}{T^{1/3}}\right]$$

It is heavily dependent on Temperature !

This would have a **positive feed-back** effect as an exothermic process.

### 3. Bethe's Solar Energy Model



The energy releasing



The final reaction product may  ***${}^7\text{Li}$***  or ***T and  ${}^4\text{He}$*** ,  
The energy would be released by the kinetic of  
these particles.





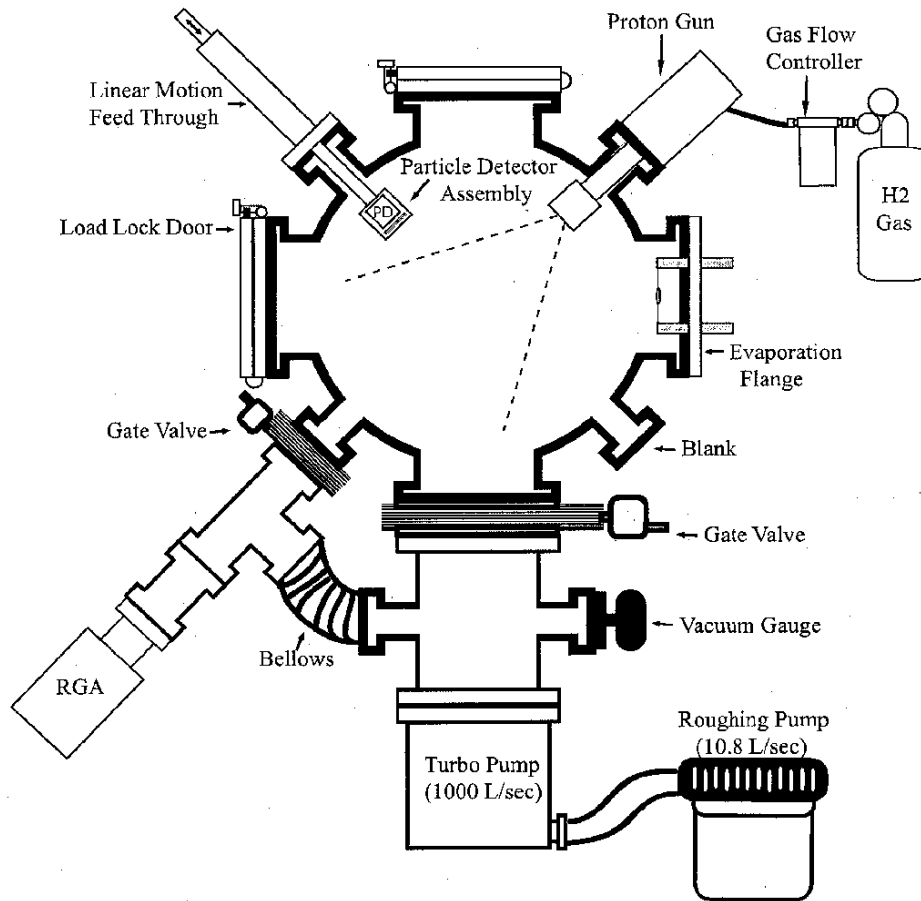
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# (10) International Publication Number WO 2014/189799 A9

(54) Title: HYDROGEN-LITHIUM FUSION DEVICE

## SERIES 23 & 24 REACTION CHAMBER COMPONENTS



(57) Abstract: The Hydrogen-Lithium Fusion Device (HLFD) includes a plasma generator that generates proton-lithium plasma within a reaction chamber. The plasma generator includes a proton source and lithium source. In one implementation, bias voltage is applied within the reaction chamber. The bias voltage enables protons to fuse with lithium ions in the proton-lithium plasma, whereby energetic helium ion fusion byproducts are produced. Multiple configurations of reaction chambers containing protons and lithium ions under conditions that yield proton-lithium fusion are disclosed.

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